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## Short Course 07: PET Kinetic Modeling and Parametric Imaging

Instructors: RN Gunn, M Normandin, GB Wang

# Total-Body PET Kinetic Modeling and Applications

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University of California Davis Health

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October 16, 2021

# Short-Course Agenda

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- 08:00 a.m. Roger Gunn (Invicro & ICL):  
Basics of dynamic PET quantification / Compartment modeling
- 09:30 a.m. Marc Normandin (MGH):  
Graphical and linearized models / Reference-tissue modeling methods
- 11:15 a.m. Guobao Wang (UCD):  
Total-body PET kinetic modeling and parametric imaging / potential applications
- 12:30 p.m. Q&A

# Disclosure

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- University of California Davis has a revenue sharing agreement and a research agreement with United Imaging Healthcare (UIH)

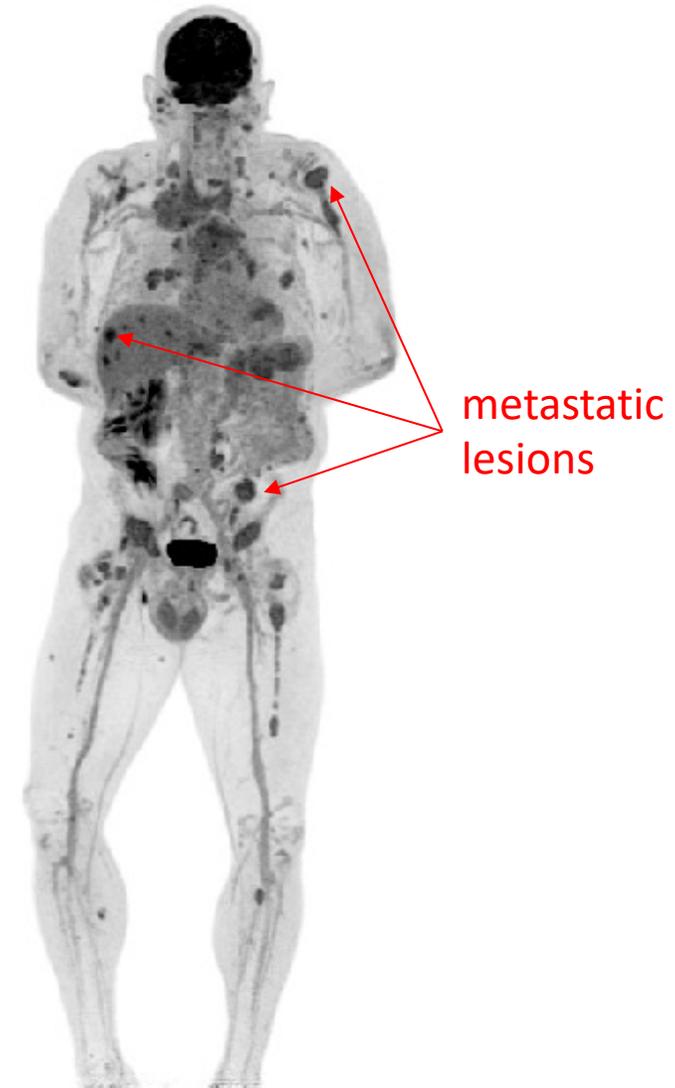
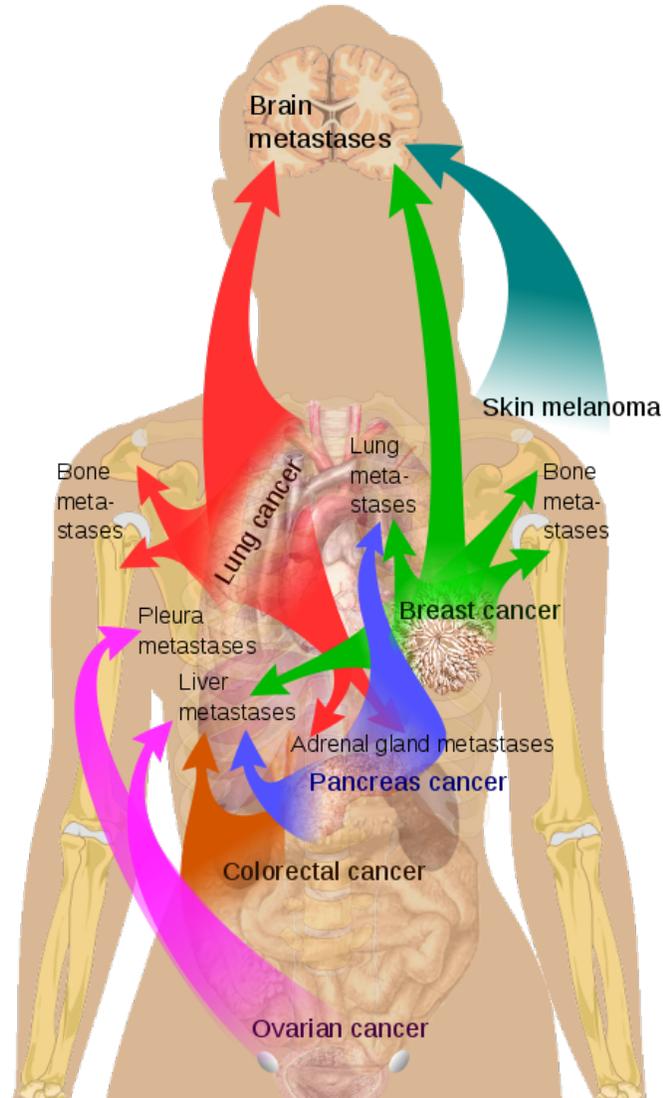
# Lecture Outline

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- I. Dynamic whole-body PET imaging on conventional short scanners
  - Whole-body Patlak parametric imaging
  
- II. Total-body PET kinetic modeling and parametric imaging with long scanners
  - Benefits of total-body PET for kinetic modeling
  - Technical challenges and solution
  - Comparison of compartmental modeling with Patlak plot
  
- III. Potential benefits/applications of total-body parametric imaging

# Why Do We Need Whole-Body Imaging?

- Example:  
metastatic cancer

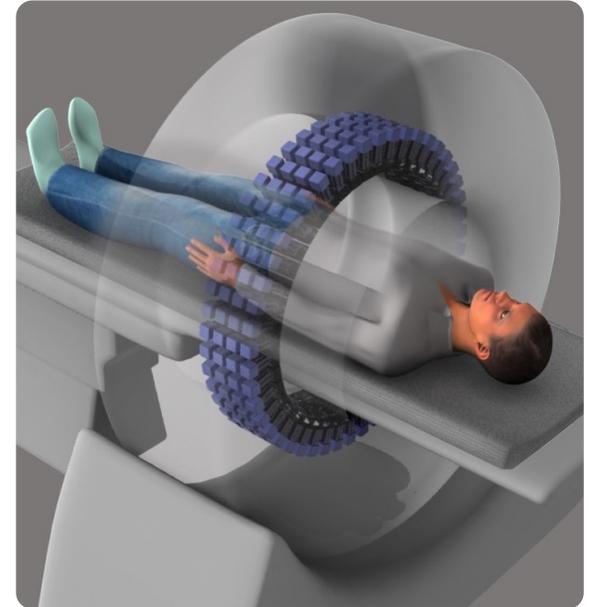


<https://en.wikipedia.org/wiki/Metastasis>

# Axial Length of Standard Clinical PET Scanners

- Standard clinical PET scanners commonly have an axial length of 15-30 cm

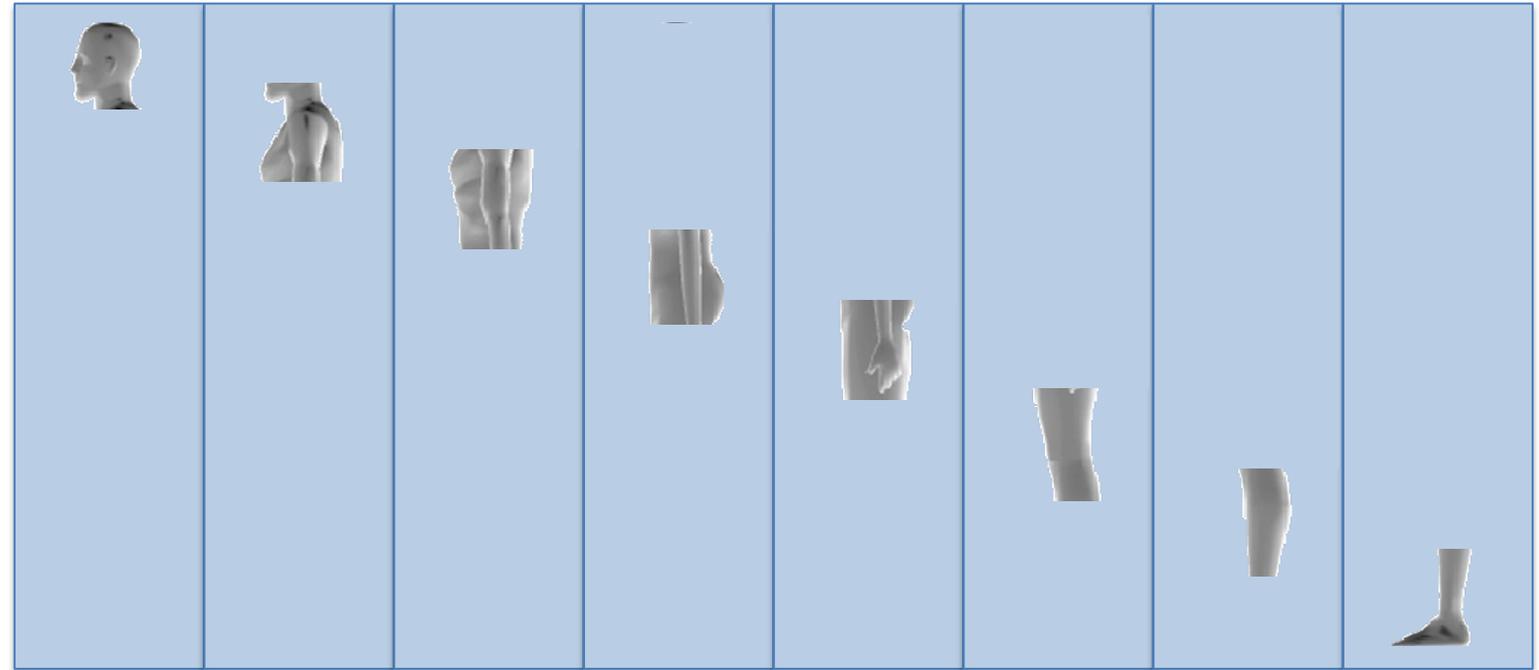
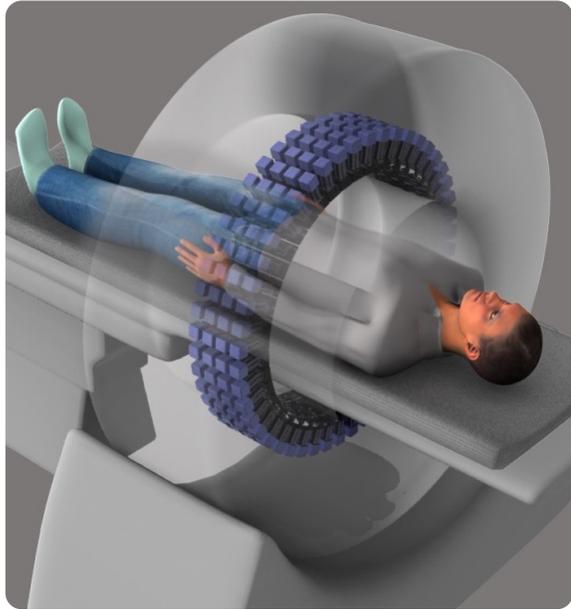
PET Scanner	Year coming into the market	Axial length (cm)
GE Discovery 690	2010	15.9
Philips Vereos	2018	16.4
GE Discovery MI (5-ring)	2018	25
Siemens Biograph Vision	2018	26
Canon Cartesion Prime	2019	27
UIH uMI780	2019	30



- However, adult human height is about 1.5-2 m

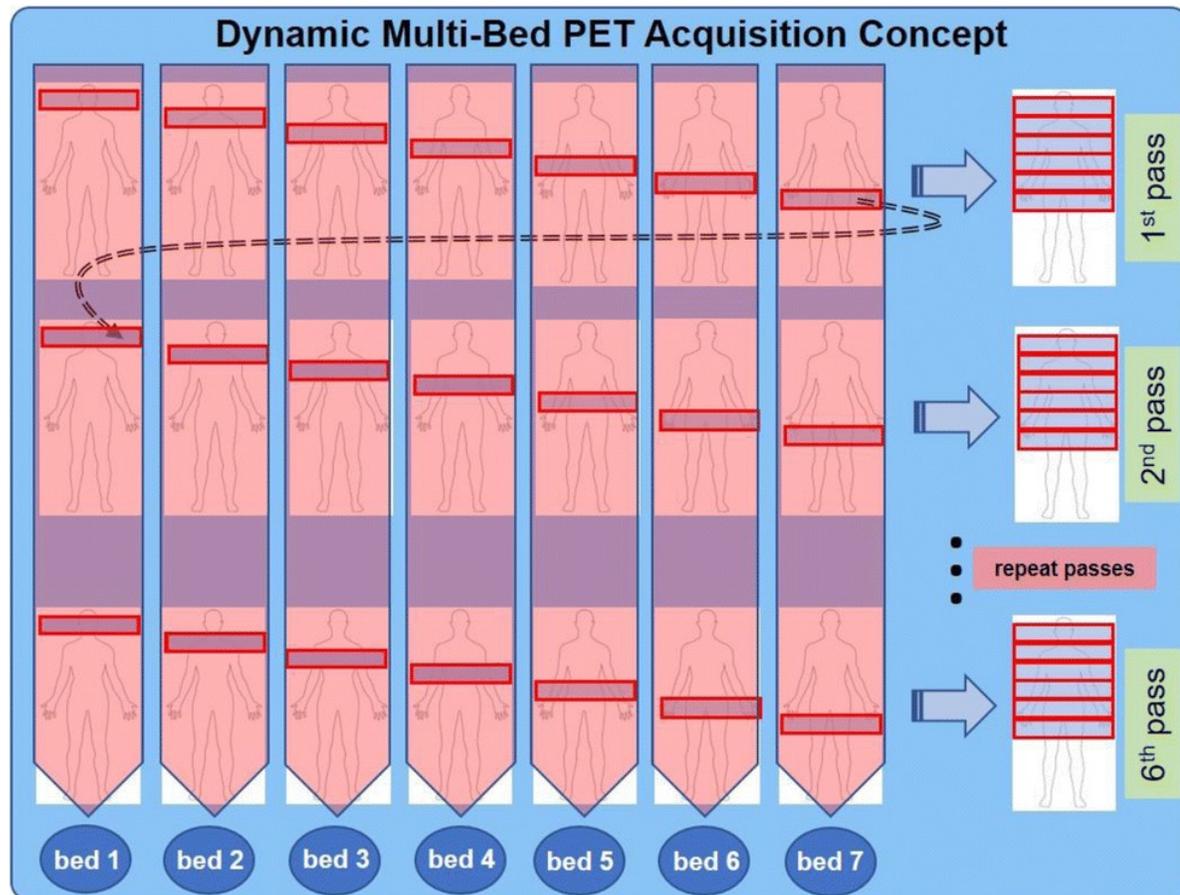
# Implementation for Whole-body PET Imaging

- A whole-body scan by a conventional PET scanner requires **multiple bed positions**



Each takes 2-3 minutes, resulting in a total of 10-20 minutes

# Dynamic Whole-Body (WB) PET Imaging

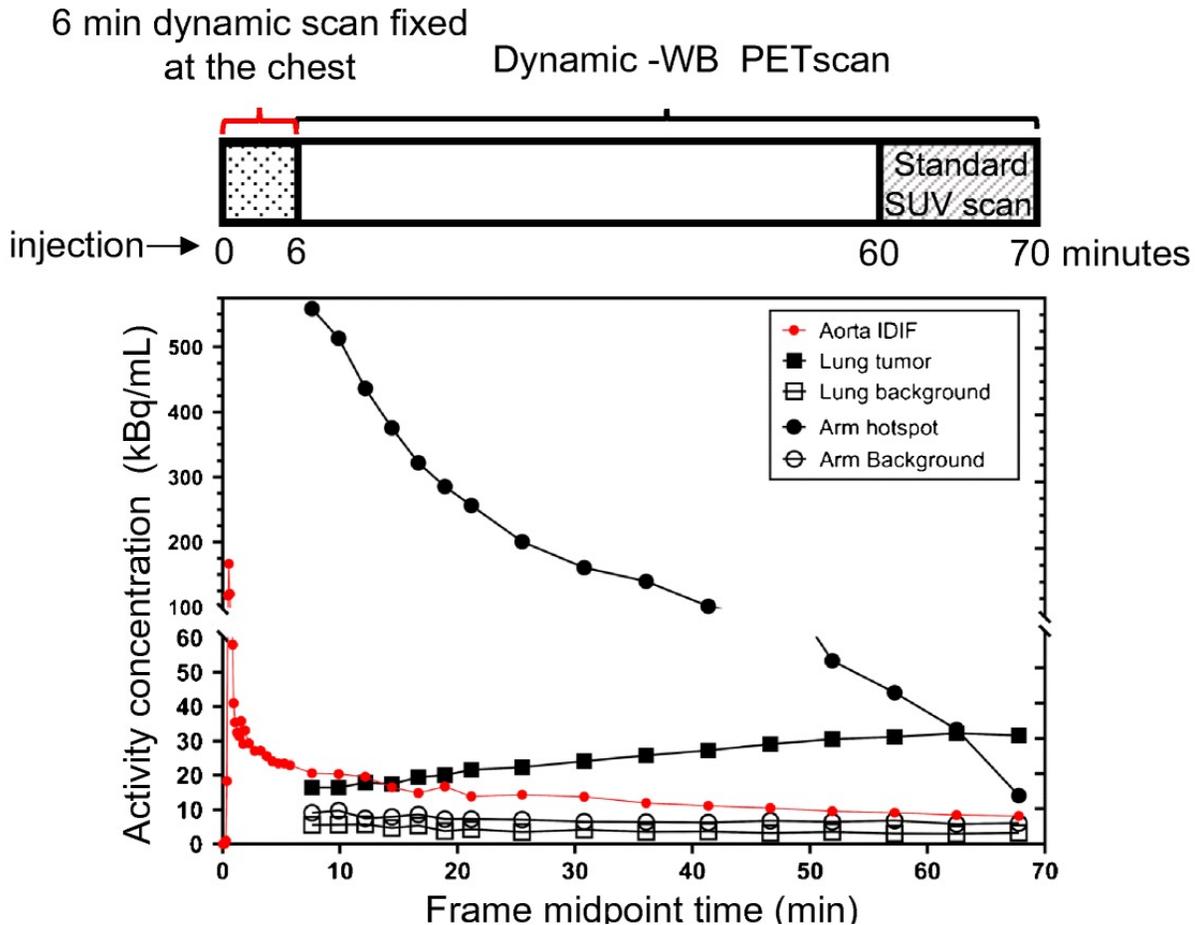


- Dynamic scan of whole body
  - Multi-bed positions
  - Two or multiple passes
  - Mainly late-phase dynamic data
- Blood input function
  - By a short dynamic scan (e.g., 6 minutes) with the bed fixed at the **chest** region
  - or by using a population-based input function

N Karakatsanis *et al.* PMB 2013; Rahmim *et al.* EJNMMI 2019

Yao *et al.* Med Phys 2020; Wu *et al.* Med Phys 2021

# Dynamic WB PET Imaging: Advantages and Limitations



AH Dias *et al.* EJNMMI 2020

- Advantages:
  - Implementable on all existing commercial PET scanners
- Limitations:
  - Limited temporal resolution
  - Lost early-dynamic data for most organs
- But it still enables whole-body Patlak parametric imaging

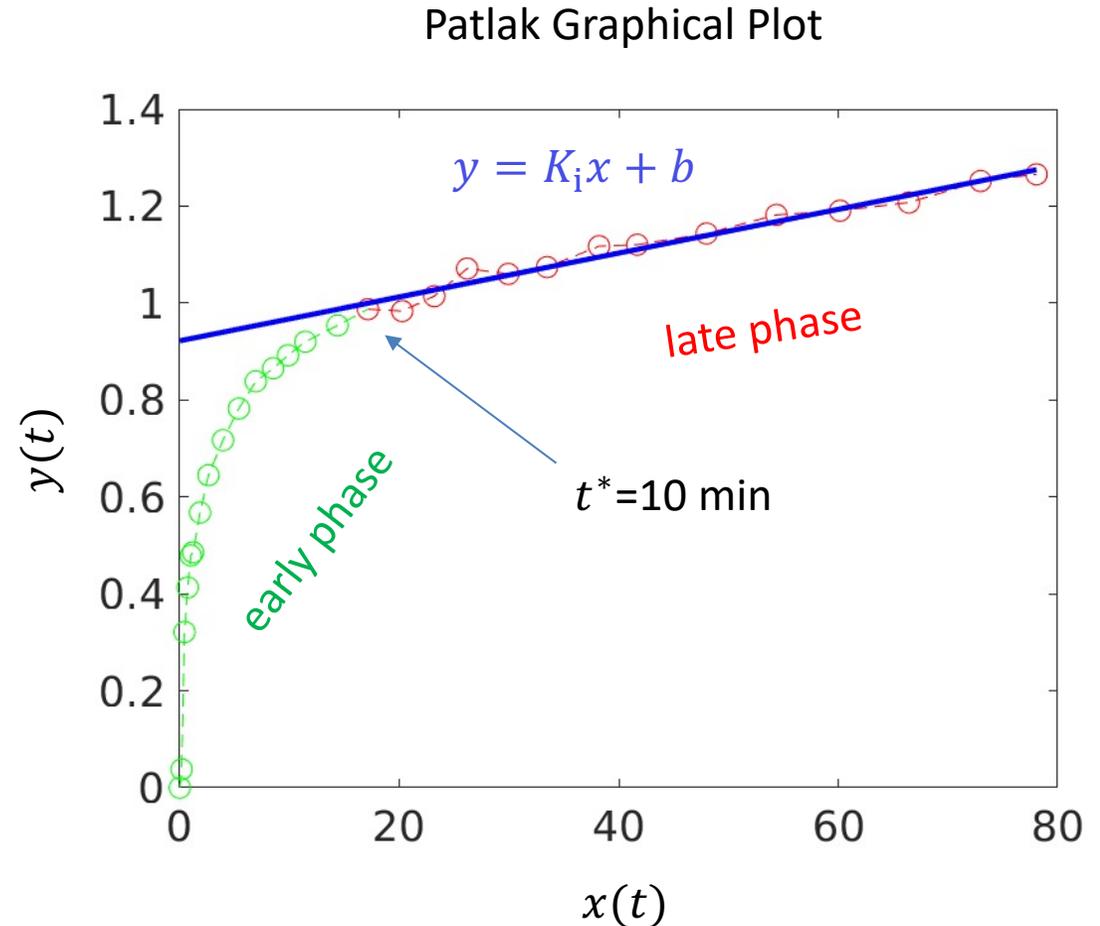
# Patlak Graphical Plot

- Model equation (Patlak *et al.* JCBFM 1983):

$$\frac{C_T(t)}{C_p(t)} = K_i \frac{\int_0^t C_p(\tau) d\tau}{C_p(t)} + b, \quad t > t^*.$$

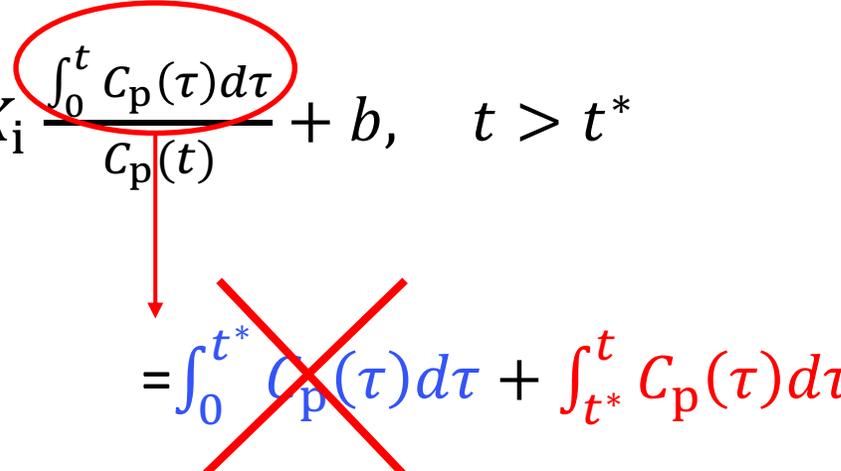
$y(t)$                        $x(t)$

- No early-phase data of  $C_T(t)$  is needed
- Observations (Zhu *et al.* TMI 2014):
  - A linear inverse problem with two unknown kinetic parameters ( $K_i, b$ )
  - In theory, only two time points are needed to solve the problem
- High temporal resolution is not necessary



# Relative Patlak Plot

- Observation: Only the **integral** of the early phase of  $C_p(t)$  is needed by the Patlak plot

$$\frac{C_T(t)}{C_p(t)} = K_i \frac{\int_0^t C_p(\tau) d\tau}{C_p(t)} + b, \quad t > t^*$$

$$= \int_0^{t^*} C_p(\tau) d\tau + \int_{t^*}^t C_p(\tau) d\tau$$

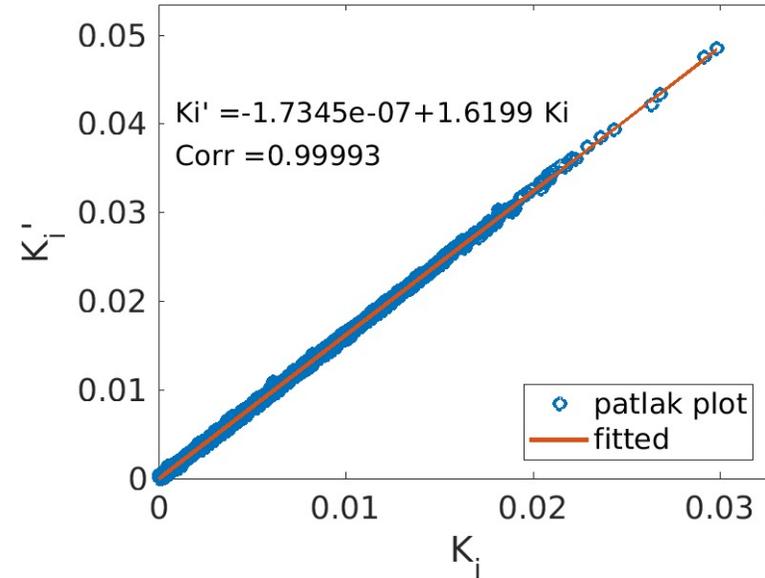
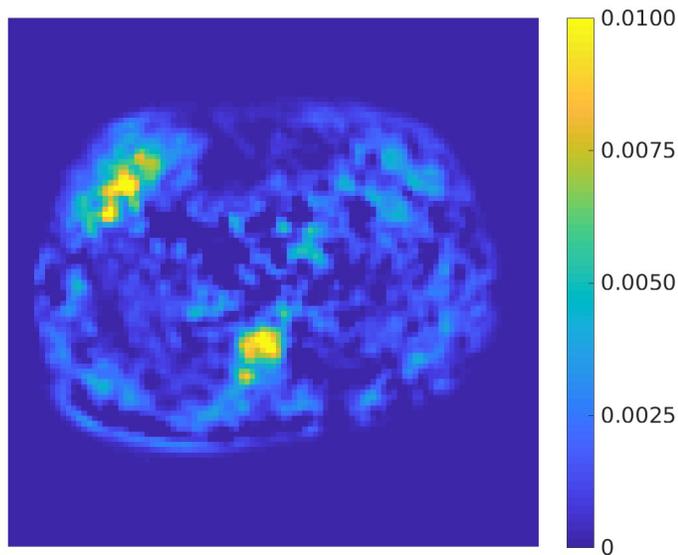
- Any error in the early-phase integral only introduces a global scaling factor in the the Patlak slope image
- Relative Patlak plot

$$\frac{C_T(t)}{C_p(t)} = K_i' \frac{\int_{t^*}^t C_p(\tau) d\tau}{C_p(t)} + b', \quad t > t^*$$

# Difference between Standard and Relative Patlak Slopes: Global Scaling

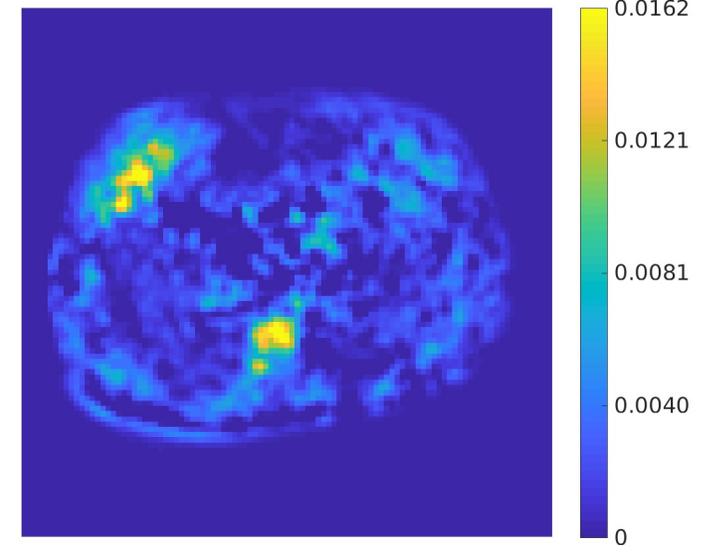
Standard Patlak plot

$K_i$



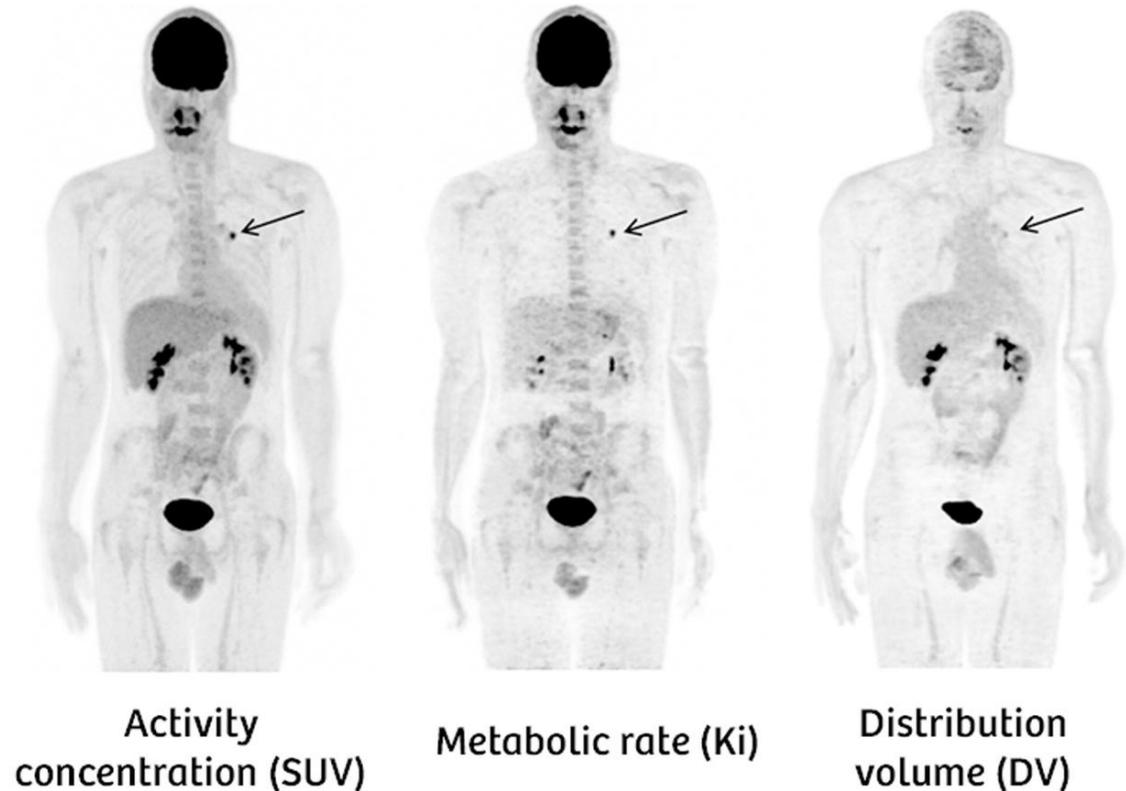
Relative Patlak plot

$K_i'$



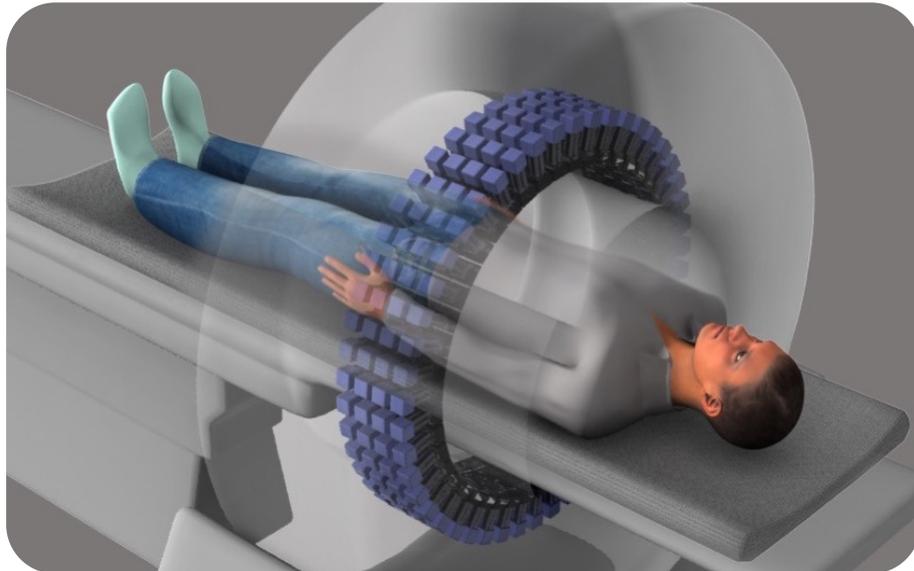
# Patlak Parametric Imaging Became Available on Commercial PET Scanners

- Siemens implemented the whole-body Patlak parametric imaging (Hu *et al.* IEEE-TRPMS 2020)
- Scan protocol: multibed multi-pass scan (Karakatsanis *et al.* PMB 2013)
- Direct parametric reconstruction with the Nested EM algorithm (Wang & Qi PMB 2010)

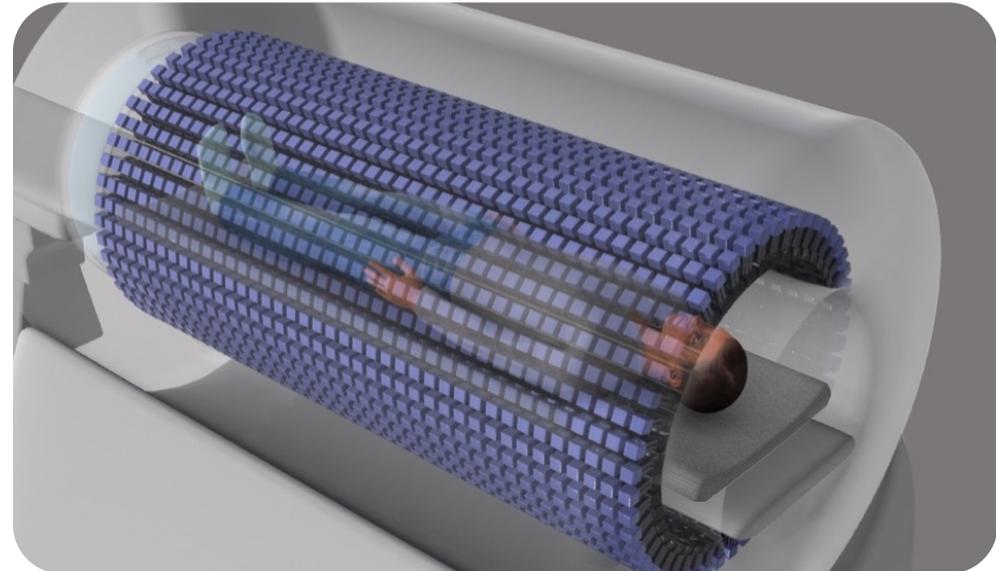


# Total-Body PET

(A) Conventional PET scanner  
(Axial FOV: 15-30 cm)



(B) EXPLORER  
(Axial FOV: 194 cm)



Total-body PET provides unprecedented photon detection sensitivity and enables simultaneous dynamic imaging of the entire body

# Long Axial FOV PET Scanners

UIH uEXPLORER (installed at UC Davis in 2019)



Axial FOV: 194 cm

Spencer *et al.* JNM 2021

PennPET EXPLORER



Axial FOV: 112 cm (extended)

Karp *et al.* JNM 2020

Siemens Biograph Vision Quadra



Axial FOV: 106 cm

Alberts *et al.* EJNMMI 2021

# Benefits of Total-Body PET for Dynamic Imaging and Kinetic Modeling

- Improved sensitivity

- makes it more robust to estimate kinetic parameters



Clinical reliability

- enables dynamic PET imaging with higher temporal resolution



Probing physiology

(Badawi *et al* JNM 2019; Zhang *et al* PNAS 2021)

- Total-body coverage

- provides *full* time course of tracer activity for *all* organs

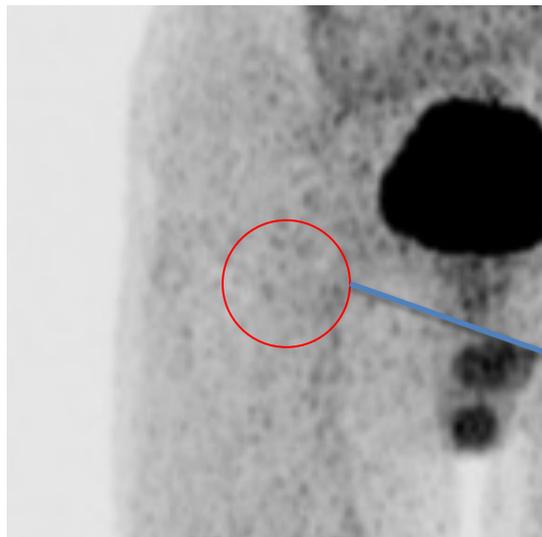


Good image-derived input function



Total-body parametric imaging of macro- and micro-kinetic parameters

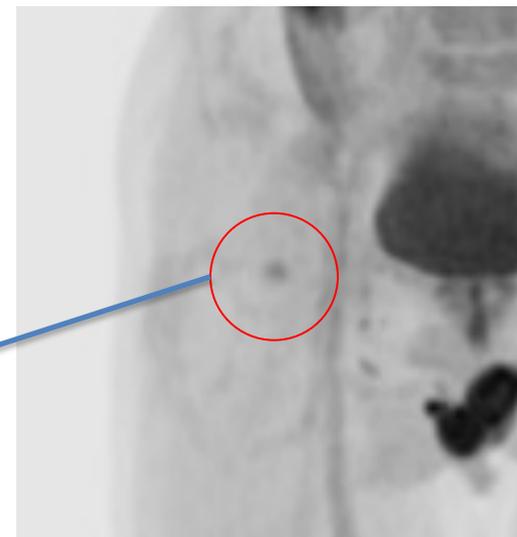
# Benefits of Total-Body PET for Dynamic Imaging: High Image Quality



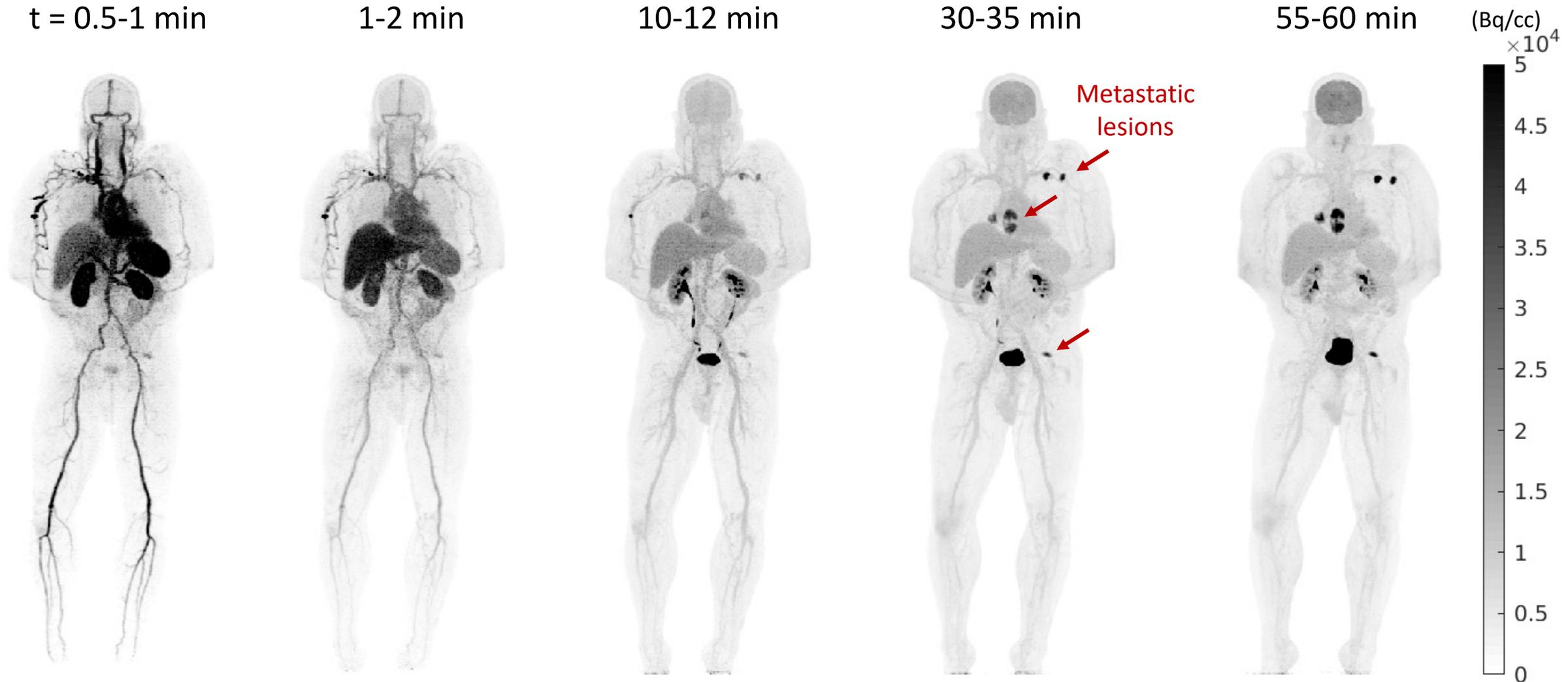
**Conventional PET (uMI 780)**  
8 beds, 2 mins/bed,  
50 min p.i.



**EXPLORER**  
20 min scan, 1 bed  
82 min p.i

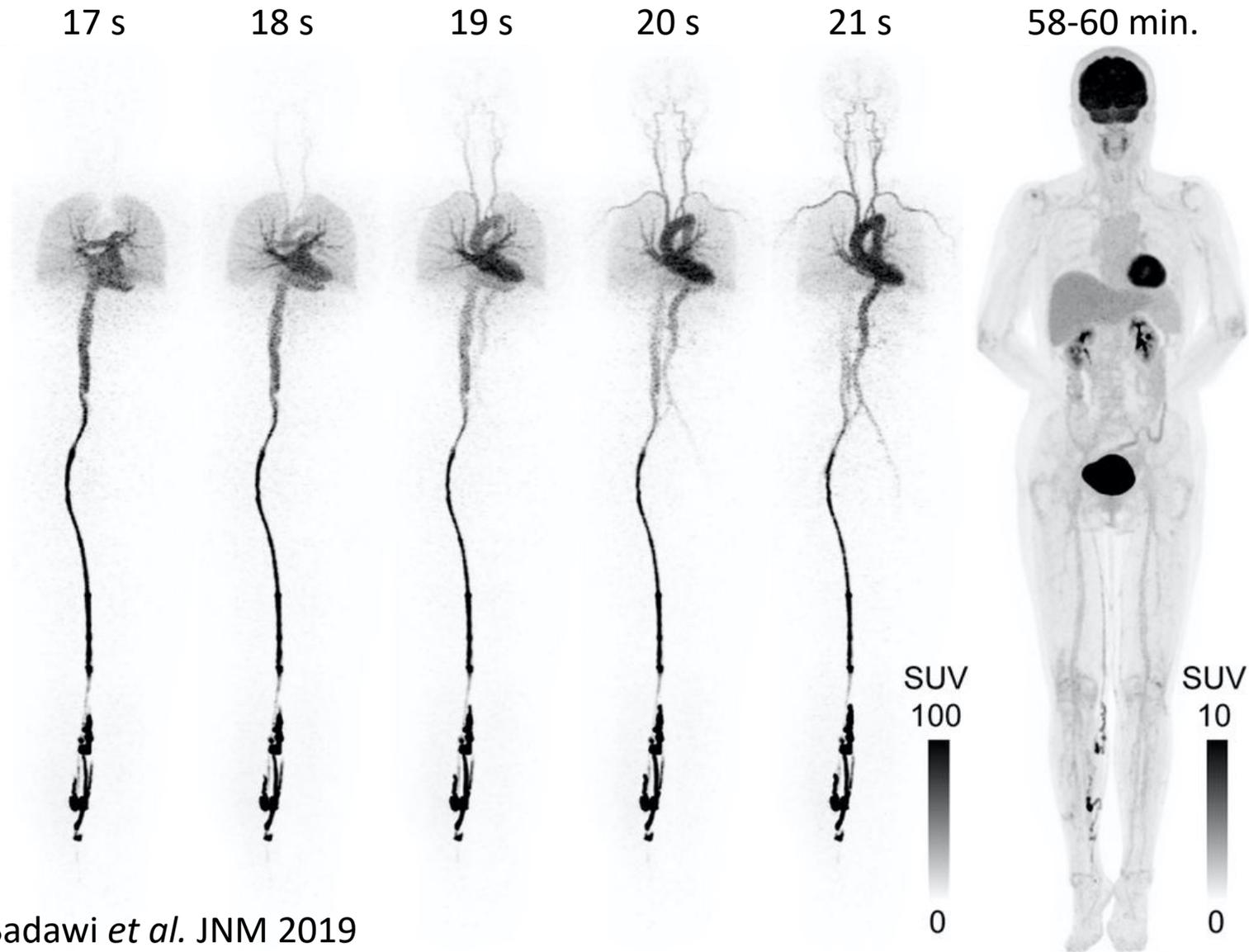


# Simultaneous Dynamic Imaging of the Entire Body on EXPLORER



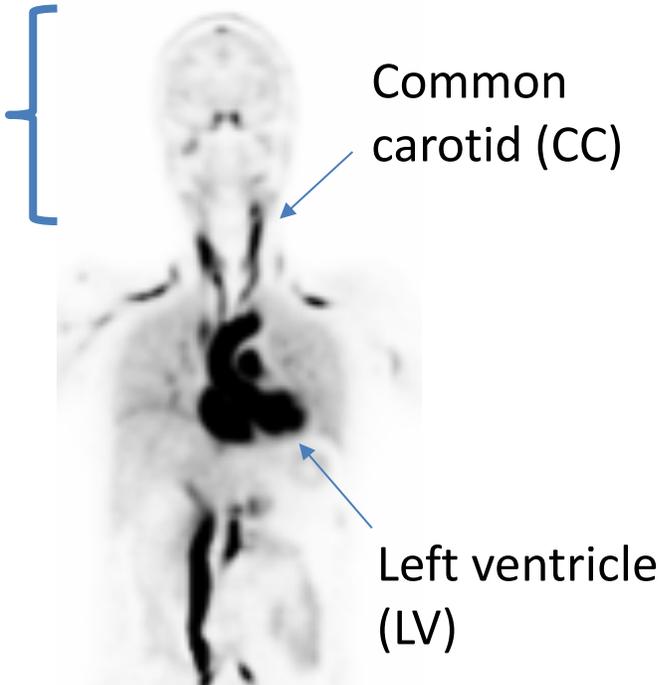
Shown are MIP (maximum intensity projection) images.

# Benefits of Total-Body PET for Dynamic Imaging: High Temporal Resolution



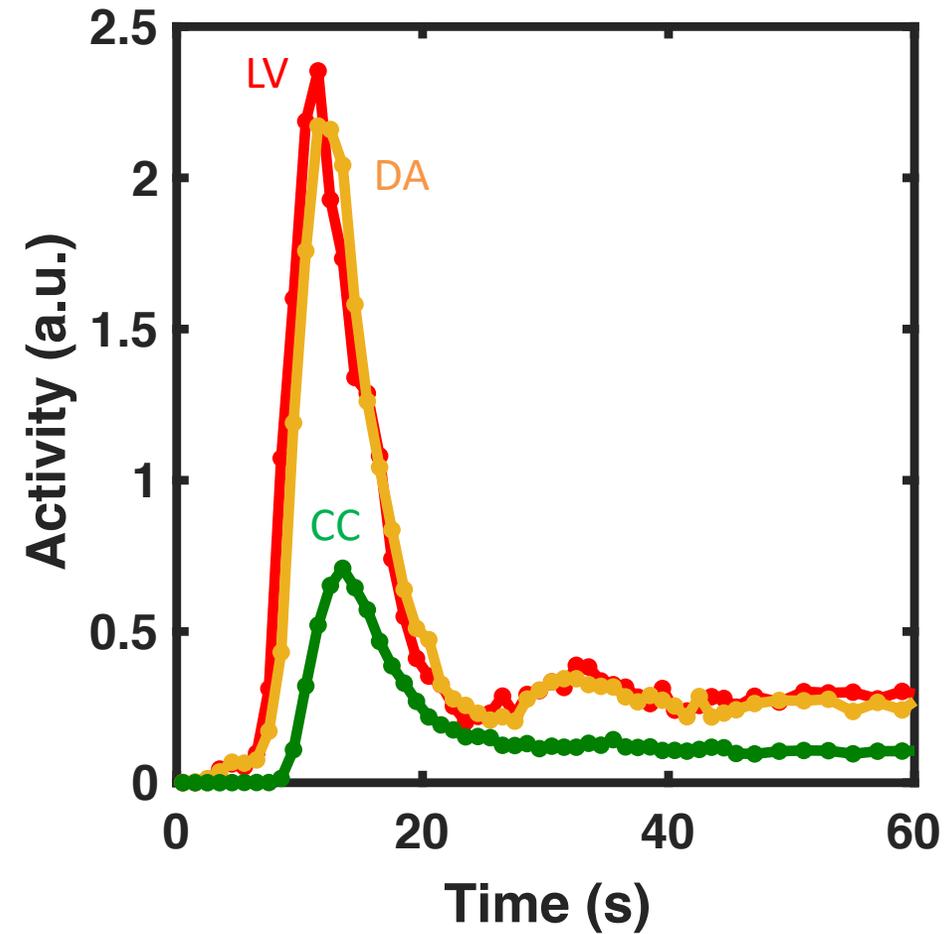
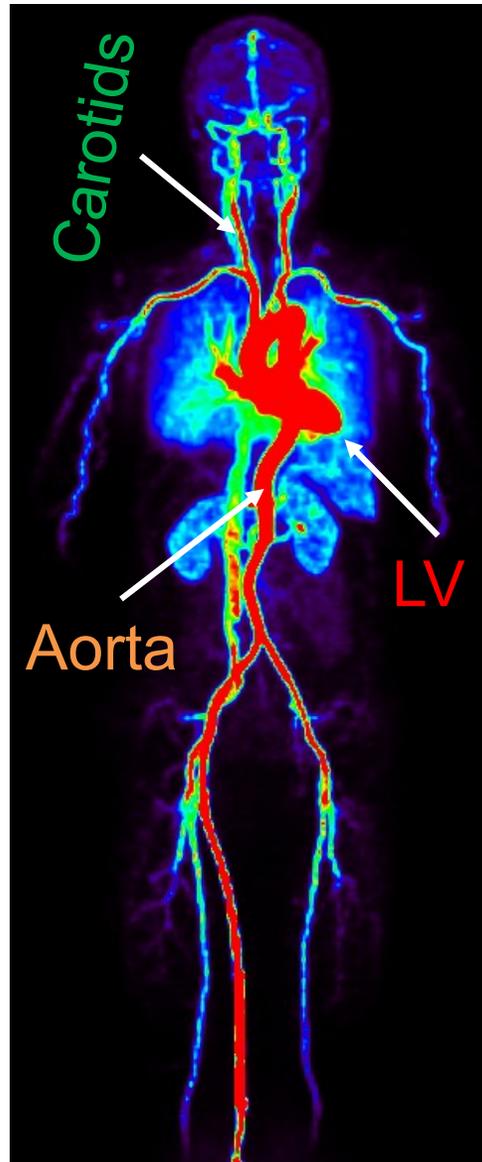
# Benefits of Total-Body PET for Kinetic Modeling: Extraction of Input Function

## Axial Coverage of Standard PET Scanners



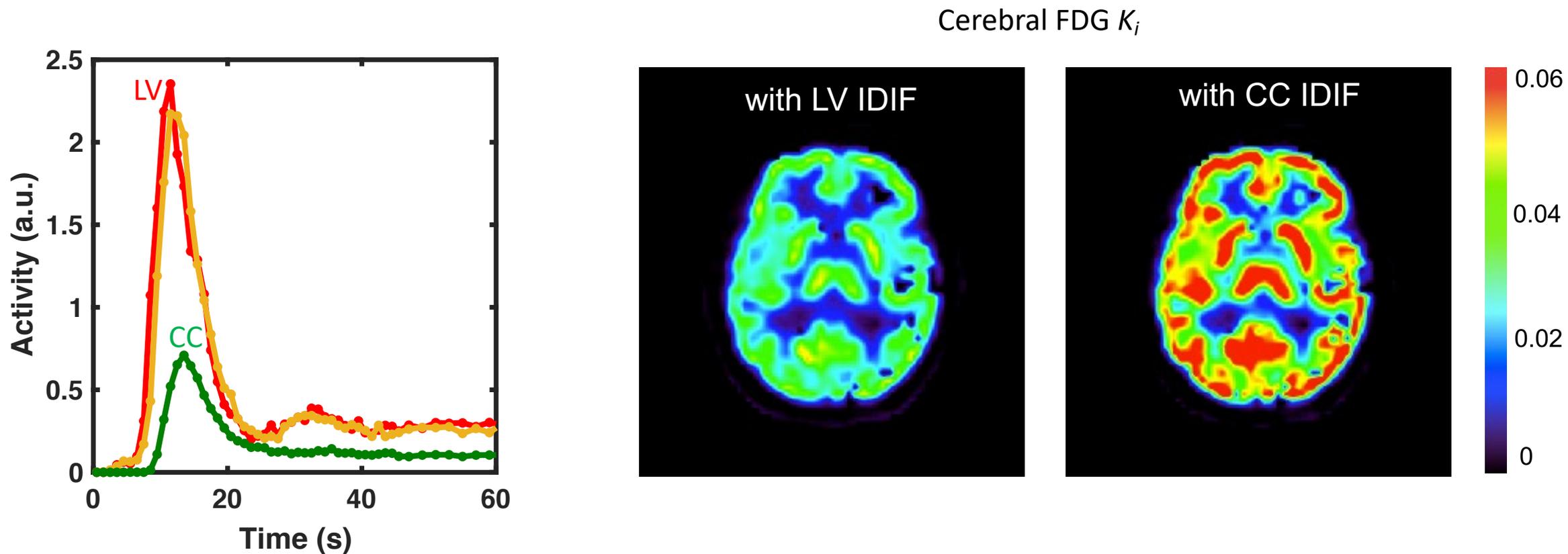
- Blood input function is conventionally obtained with invasive blood sampling
- For brain imaging, best available image-derived input function (IDIF) by conventional PET scanners is from the common carotid artery, which however suffers from severe partial volume effect
- With total-body PET, IDIF is available from a large blood pool, e.g., the left ventricle

# Image-Derived Input Functions (IDIFs) in Total-Body Dynamic PET

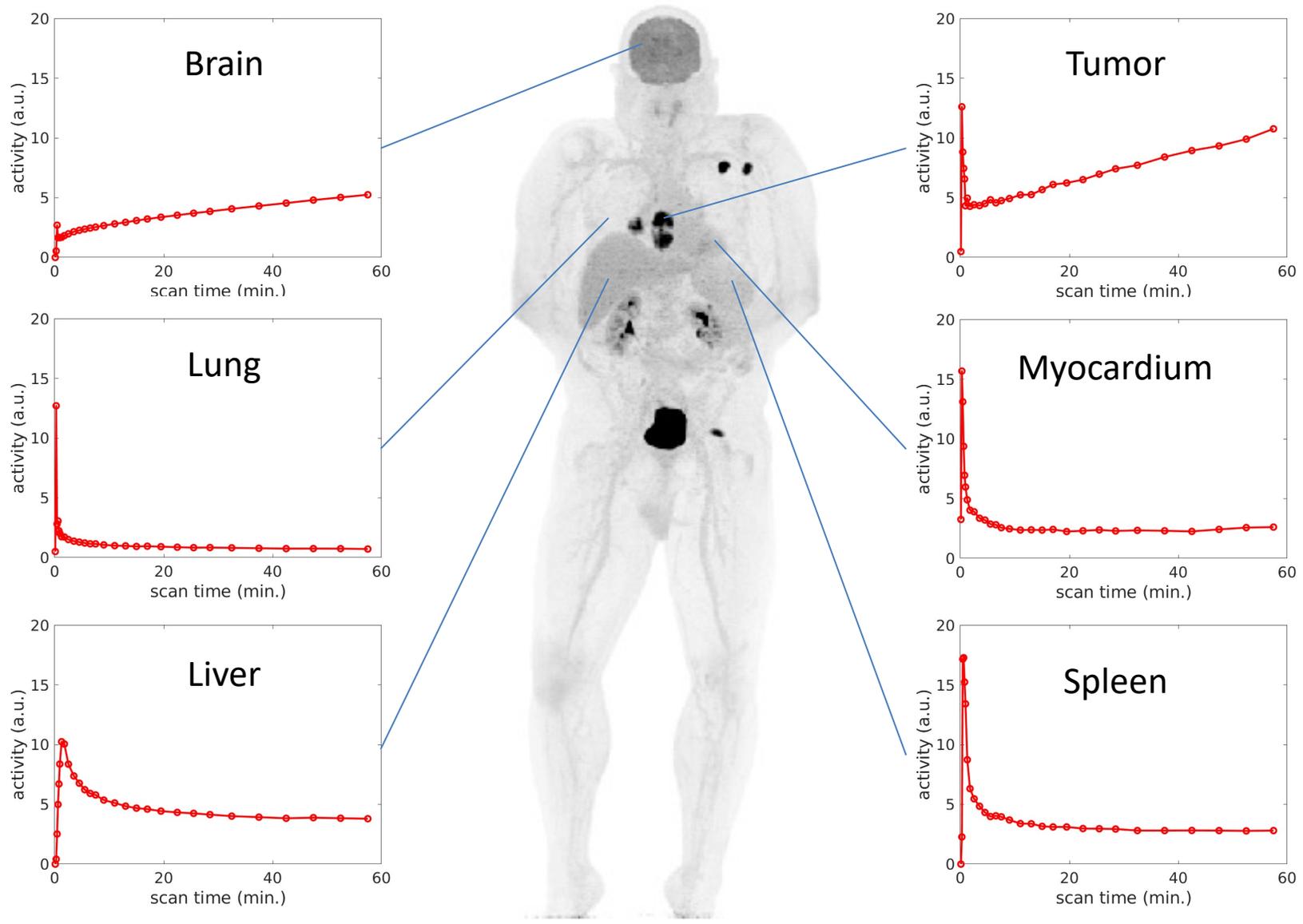


Courtesy of Elizabeth Li

# Example of Brain Parametric Imaging



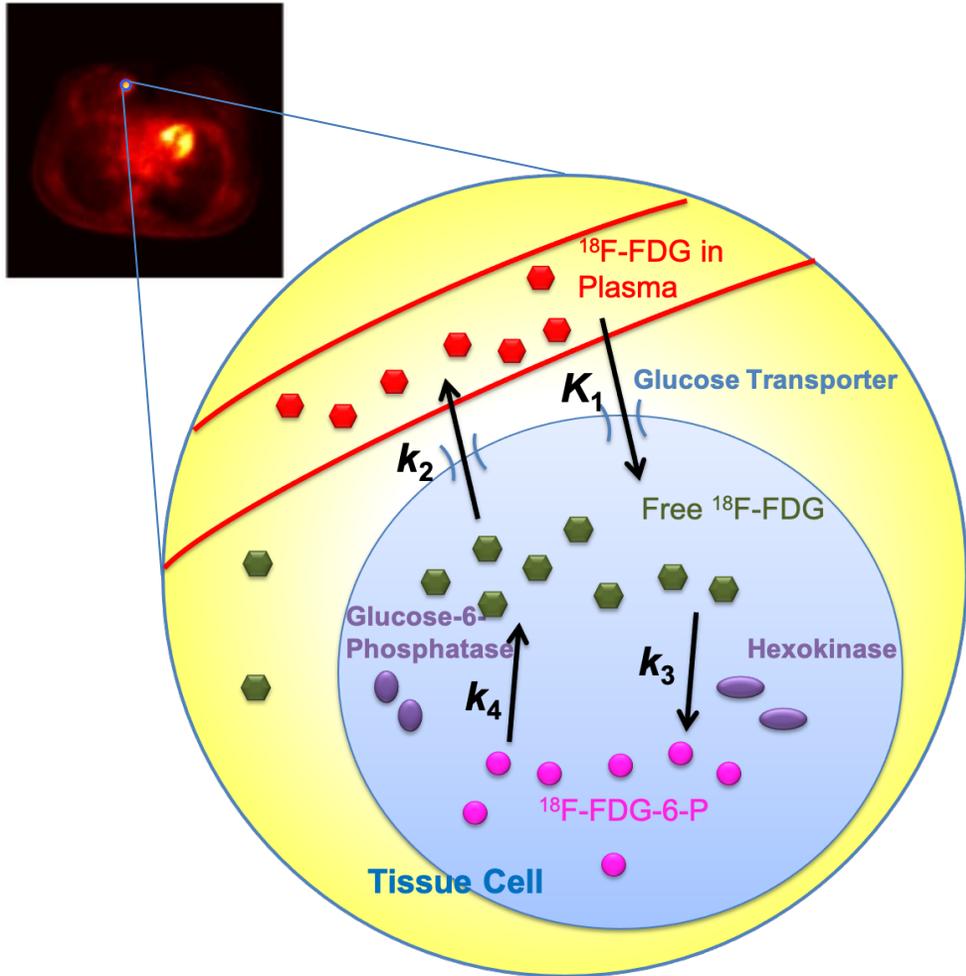
# Benefits of Total-Body PET for Dynamic Imaging : Capturing the Full Time Course of Tracer Activity in All Organs



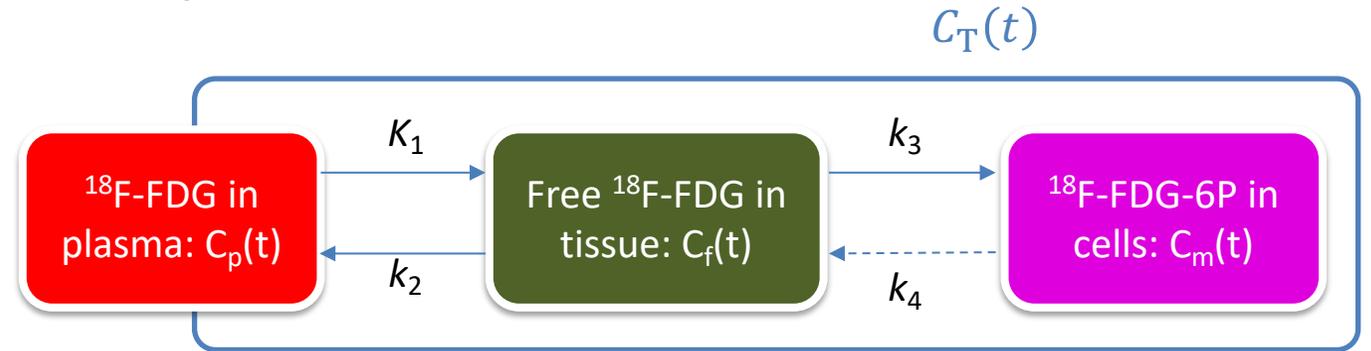
# Total-Body Patlak Parametric Imaging on EXPLORER



# Benefits of Total-Body PET for Kinetic Modeling: Parametric Imaging with Compartmental Models



- Compartmental model



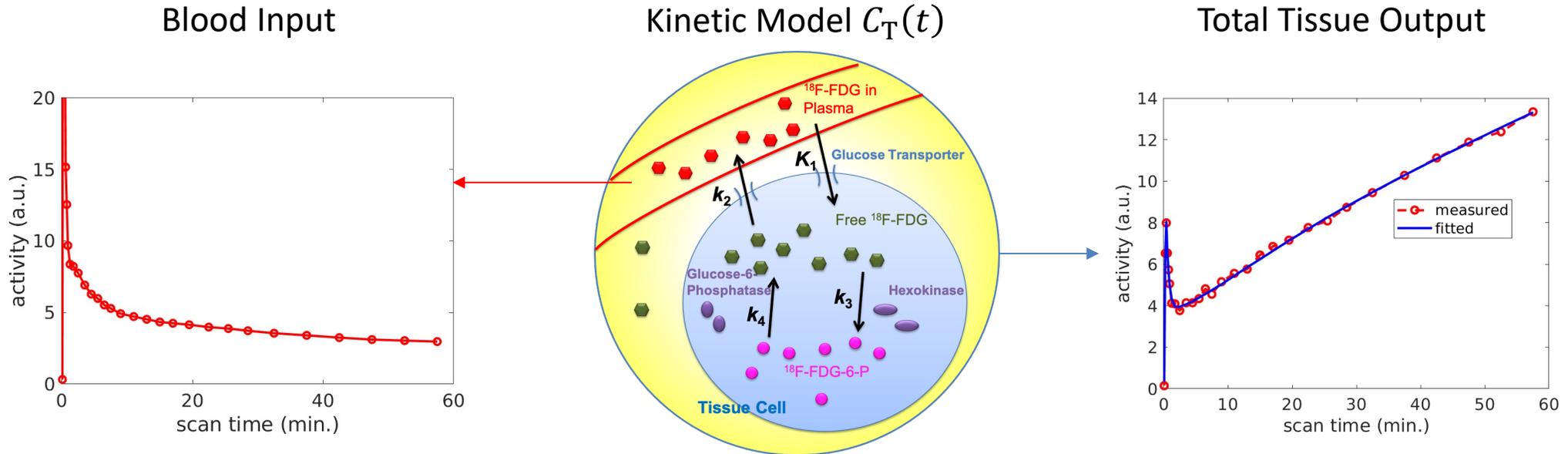
- Differential equations

$$\frac{d}{dt} \begin{bmatrix} C_f(t) \\ C_m(t) \end{bmatrix} = \begin{bmatrix} -(k_2 + k_3) & k_4 \\ k_3 & -k_4 \end{bmatrix} \begin{bmatrix} C_f(t) \\ C_m(t) \end{bmatrix} + \begin{bmatrix} K_1 \\ 0 \end{bmatrix} C_p(t)$$

- Total activity that is measured by PET is

$$C_T(t) = (1 - v_b)[C_f(t) + C_m(t)] + v_b C_b(t)$$

# Kinetic Parametric Estimation by Full Time Activity Curve (TAC) Fitting

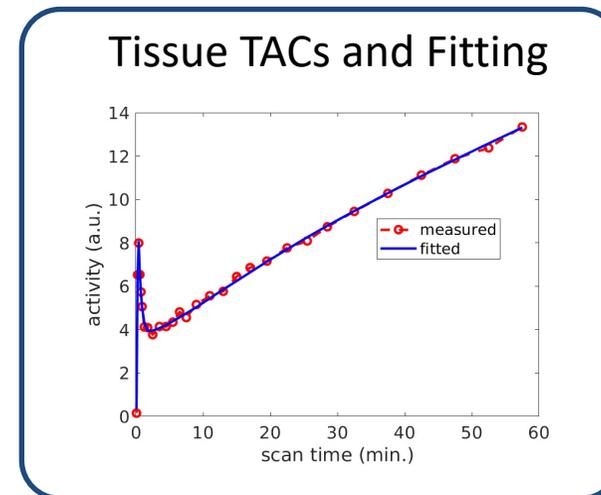
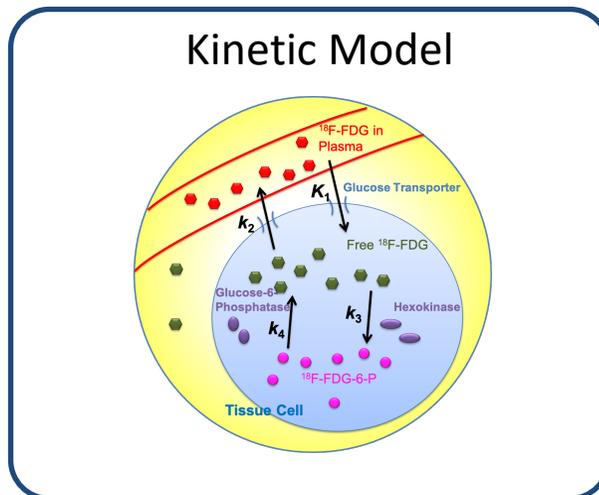
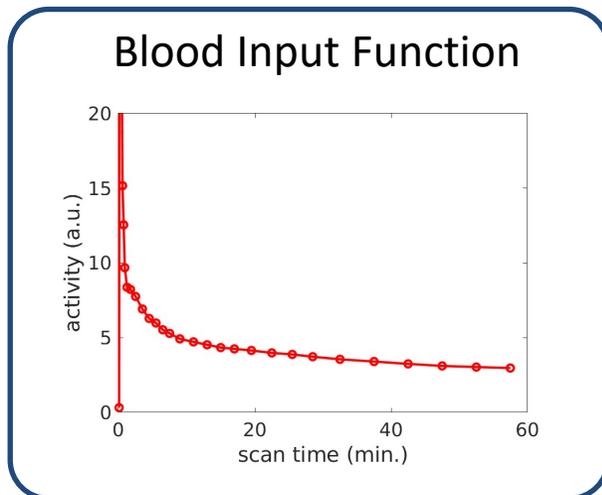


- Micro-kinetic parameters (e.g.,  $K_1$ ,  $k_2$ , ...) are estimated from TAC fitting
- Macro kinetic parameters can be calculated, e.g., for FDG:

$$\text{Net influx rate } K_i = \frac{K_1 k_3}{k_2 + k_3}; \quad \text{Initial volume of distribution } V_0 = \frac{K_1 k_2}{(k_2 + k_3)^2}$$

# Challenges of Total-Body Kinetic Modeling and Parametric Imaging

Key Components



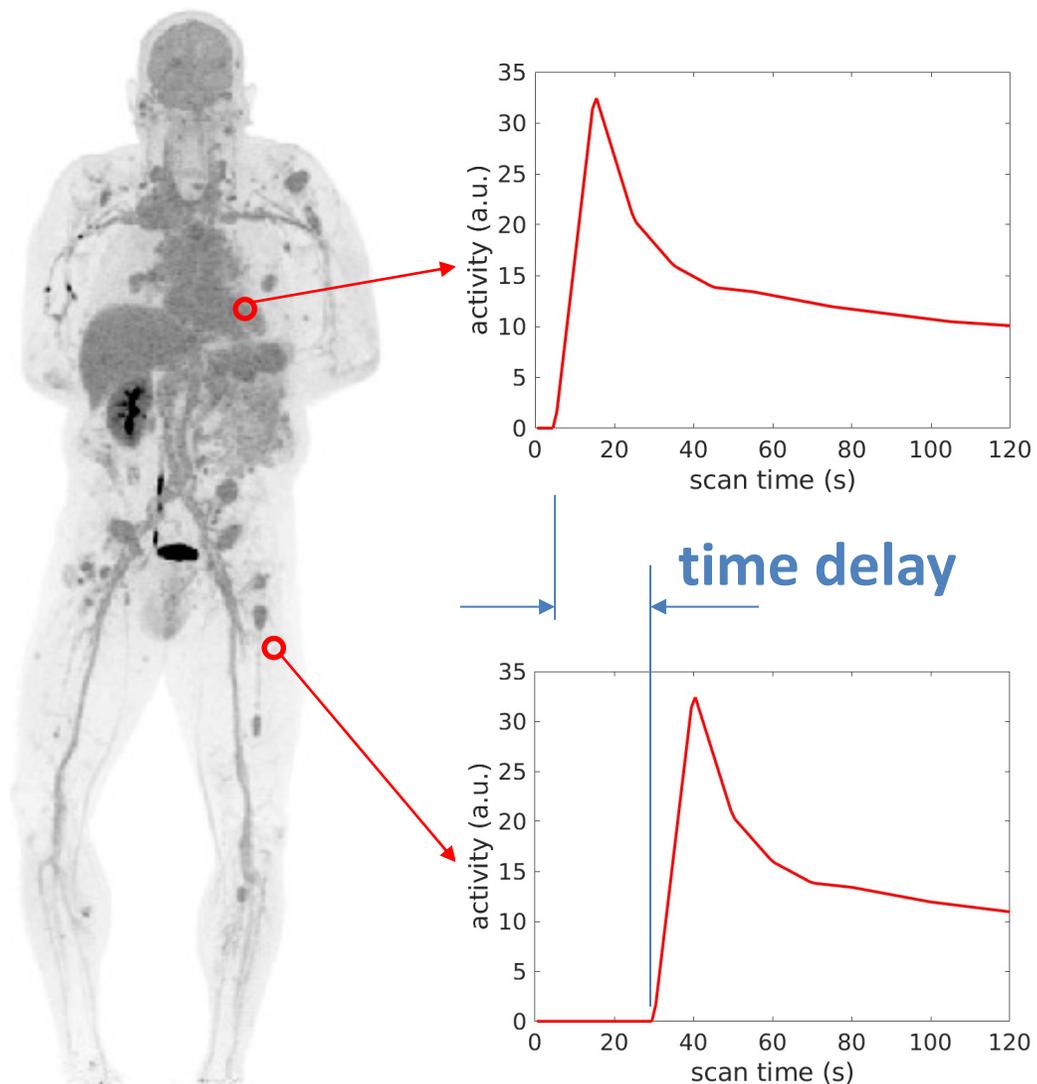
Challenges

- Time delay and dispersion correction
- Modeling of dual blood supplies (in liver, lung)
- Parent fraction correction
- Metabolite correction

- Model selection
- Identifiability
- ...

- Huge dataset
- Motion
- Local minimum
- ...

# Time Delay of the Blood Input Function



(A) IDIF extracted in left ventricle

(B) actual arrival in a tissue

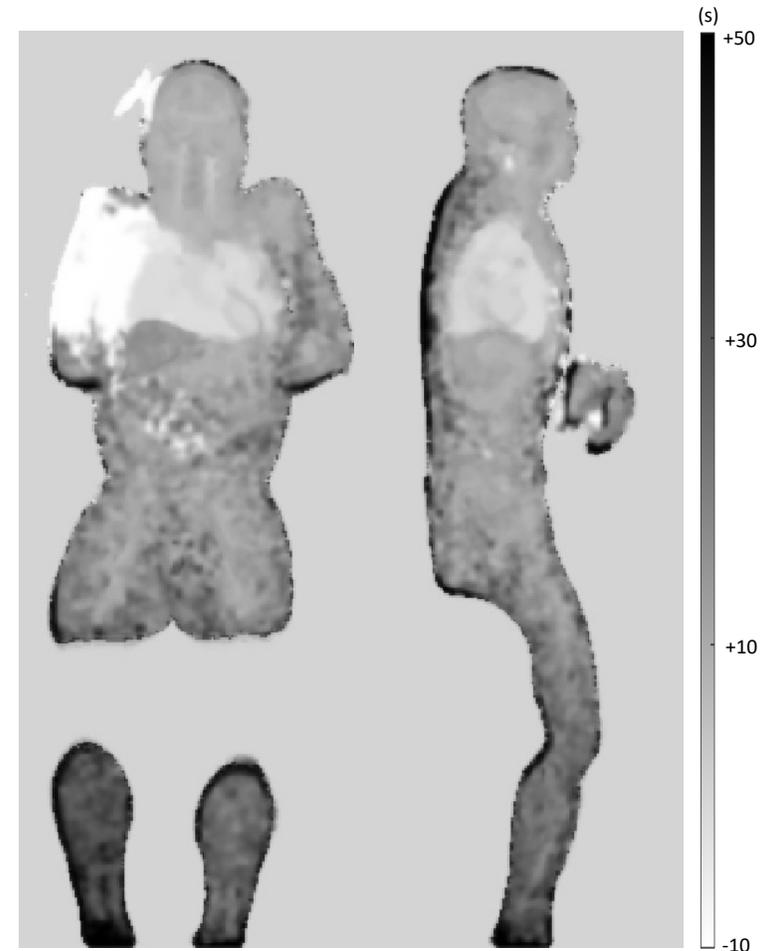
# Commonly Neglected in Parametric Imaging

- $K_i$  estimation is more dominated by the late phase instead of early phase of a dynamic scan
- Within a limited axial FOV of 15 cm of conventional PET, time delay can be just a few seconds
- Temporal resolution of dynamic PET was limited (e.g., 10-40 s/frame)
- Mainly considered to be important for estimation of fast kinetics (e.g., cerebral blood flow imaging using  $^{15}\text{O}$ -water)

# Importance for Total-Body Kinetic Modeling

- Time delay in a tissue distant from the left ventricle can be up to 50 seconds
- Metastatic lesions spread to distant organs, which can be far away from the blood pool where a blood input function is extracted
- May significantly affect the estimation of  $v_b$ ,  $K_1$  and  $K_i$

Example of time delay map estimated from a  $^{18}\text{F}$ -FDG patient scan



# Time-Delay Correction by Joint Estimation

- Model TAC without time delay

Impulse response function;  
 $\boldsymbol{\kappa} = [K_1, k_2, k_3]^T$

$$C_T(t) = (1 - v_b) \text{IRF}(t; \boldsymbol{\kappa}) \otimes C_p(t) + v_b C_b(t)$$

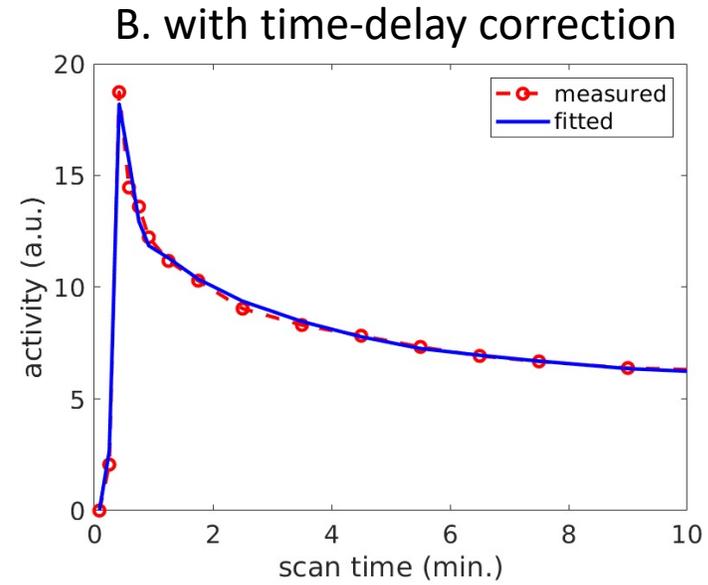
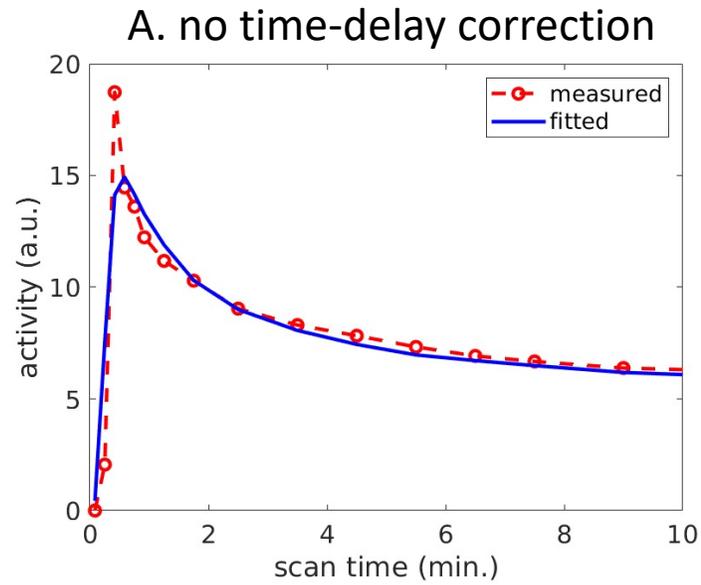
- Model TAC with time delay correction

$$C_T(t) = (1 - v_b) \text{IRF}(t; \boldsymbol{\kappa}) \otimes C_p(t - t_d) + v_b C_b(t - t_d)$$

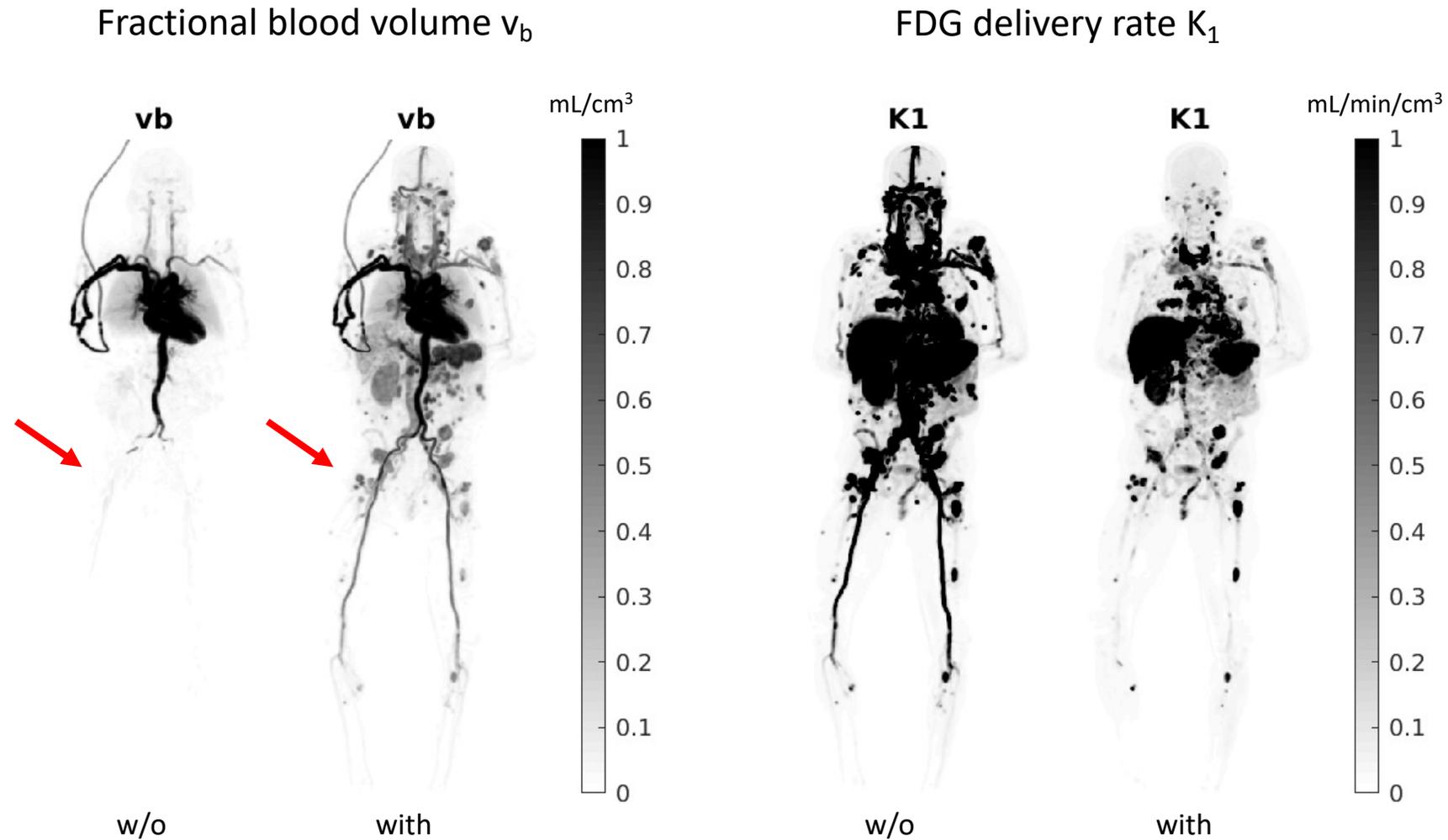
- $\boldsymbol{\theta} = [\boldsymbol{\kappa}^T, v_b, t_d]^T$  is jointly estimated via nonlinear least-square fitting:

$$\hat{\boldsymbol{\theta}} = \arg \min_{\boldsymbol{\theta}} \text{RSS}(\boldsymbol{\theta}), \text{RSS}(\boldsymbol{\theta}) = \sum_{m=1}^M w_m [\check{C}_T(t_m) - C_T(t_m)]^2$$

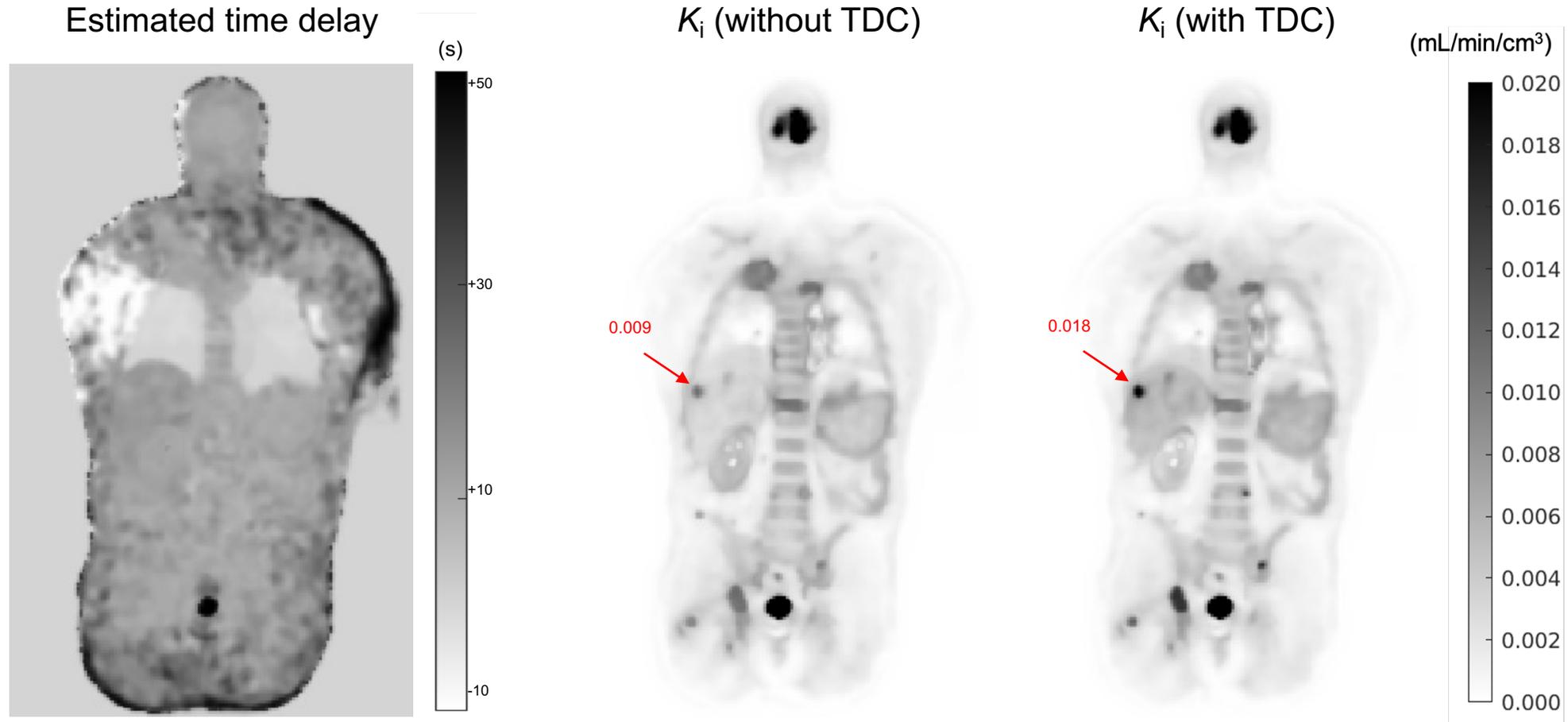
# Example of Fitting a Lesion TAC



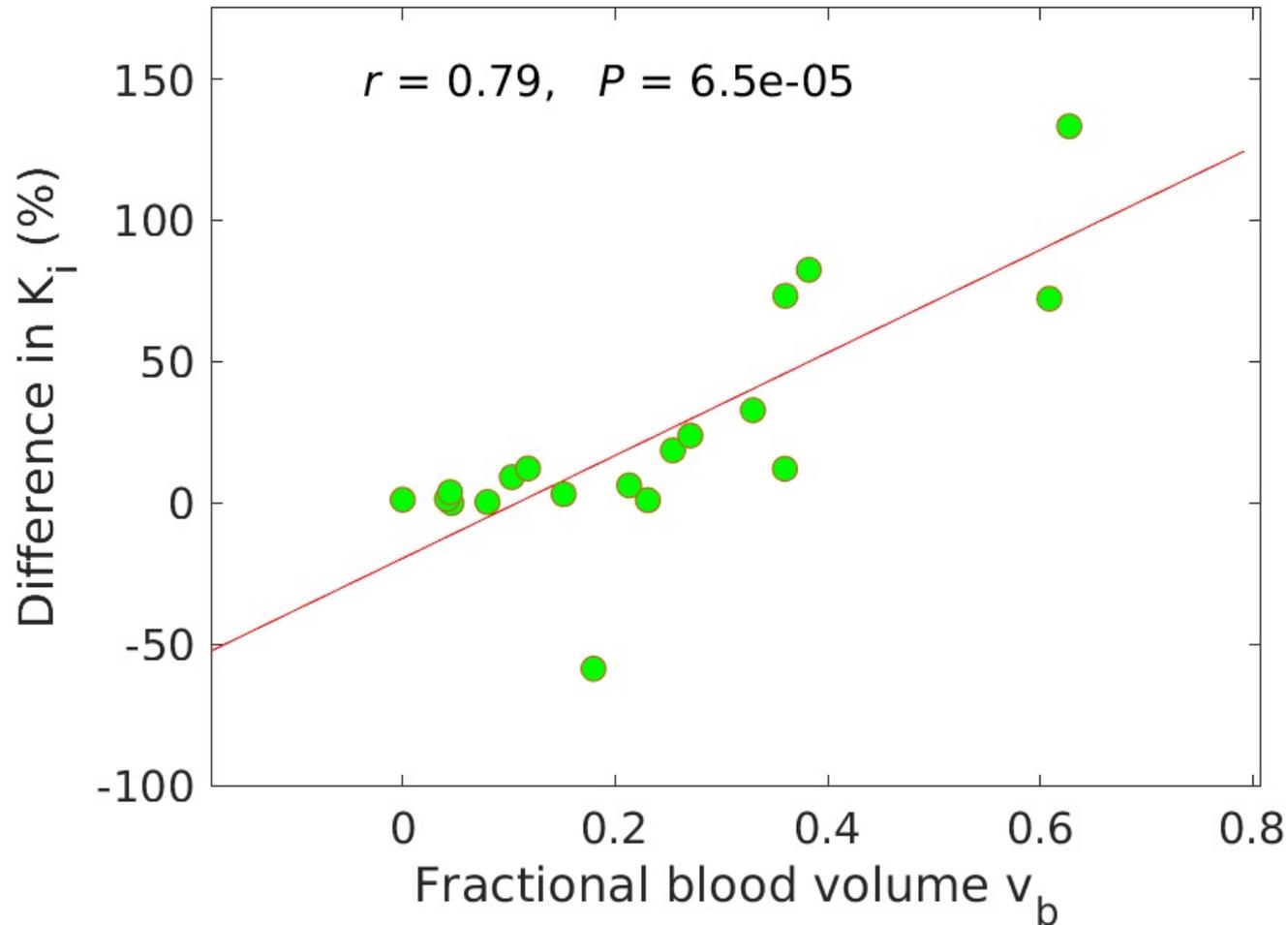
# Time-Delay Correction on Total-Body Parametric Imaging



# Time-Delay Correction (TDC) Also Impacts on FDG $K_i$



# Impact of Time Delay Correction Correlates with Blood Volume Fraction



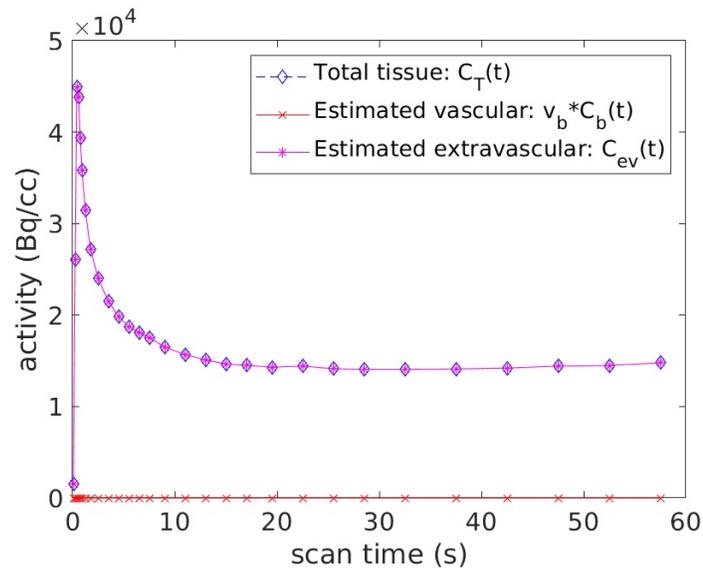
Results from 19 lesions from 5 patients with metastatic genitourinary cancer

# Why Time-delay Correction May Impact $K_i$ Estimation?

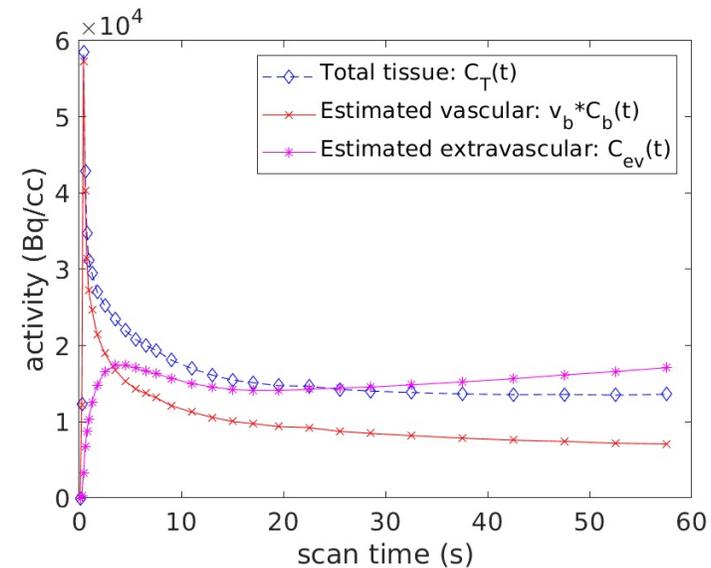
$$C_T(t) = (1 - v_b) \text{IRF}(t; \kappa) \otimes C_p(t - t_d) + v_b C_b(t - t_d)$$

$\underbrace{\hspace{10em}}_{C_{ev}(t)}$

A. No time delay estimation



B. With time delay estimation

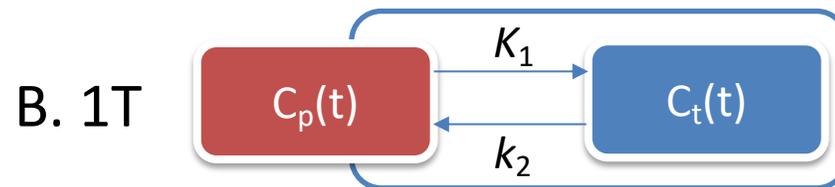
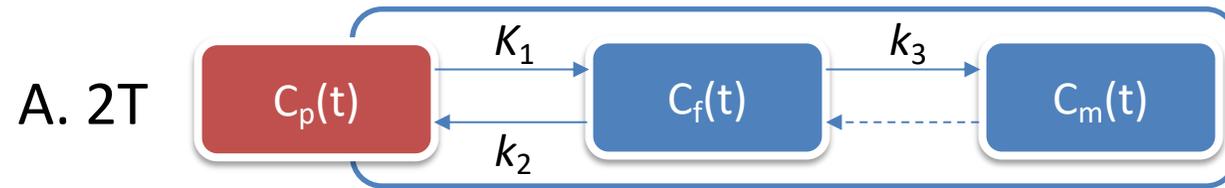


# Total-Body Model Selection

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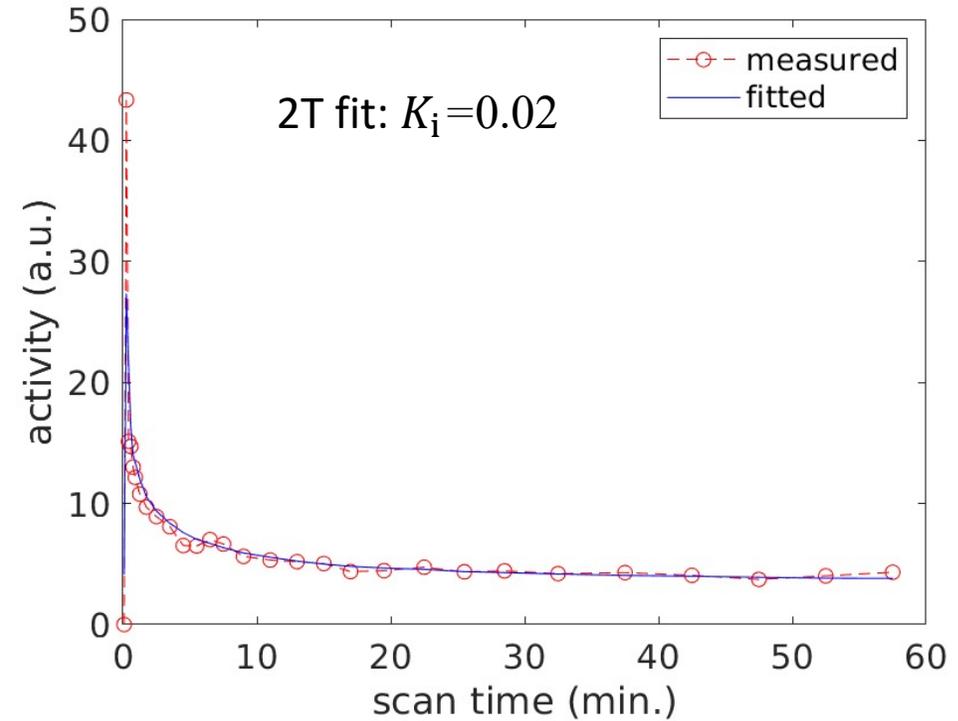
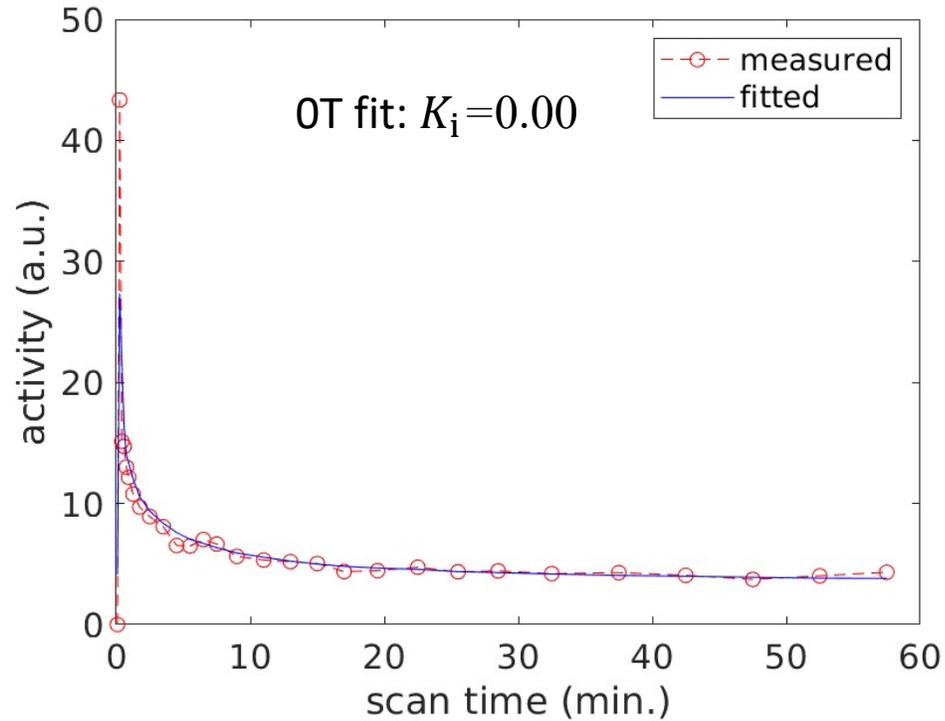
- Conventionally a fixed model is commonly used in organ-specific parametric imaging, e.g.,
  - Brain
  - Myocardium
- Total-body parametric imaging
  - Many different organs
  - Each may follow a different compartmental model

# Example of Candidate Compartmental Models



# Which Model Is the Best?

- Similar fits, but very different  $K_i$  results



# Akaike Information Criteria (AIC)

- Definition

$$\text{AIC} = M \ln \left( \frac{\text{RSS}}{M} \right) + 2n$$

Goodness of fit

Penalty on a more complex model

where  $RSS$  denotes the residual sum of squares

$$RSS = \sum_{m=1}^M w_m [\check{C}_T(t_m) - C_T(t_m)]^2$$

with  $M$  the number of frames and  $n$  the number of unknown kinetic parameters.

# AIC for Small Sample Size

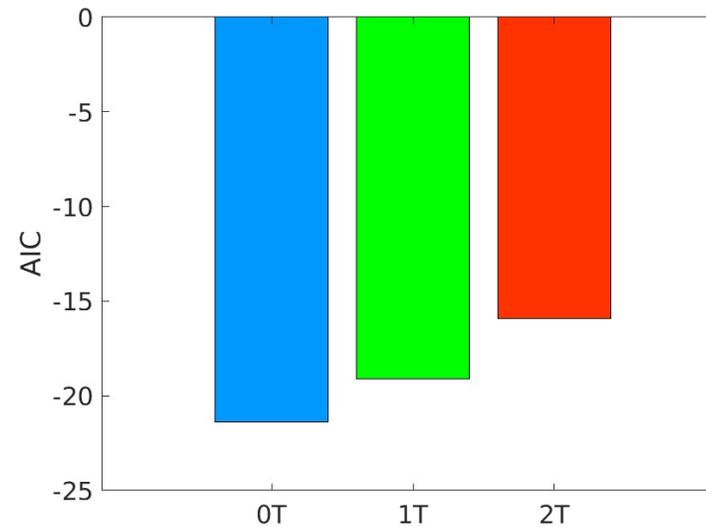
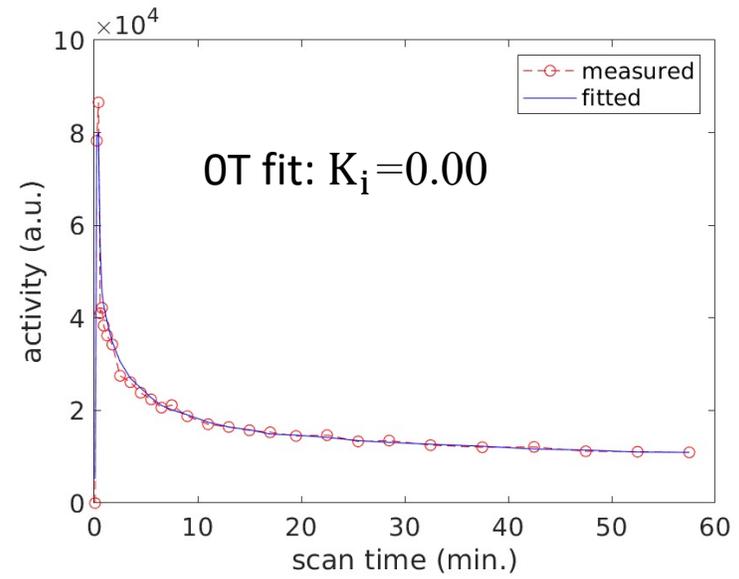
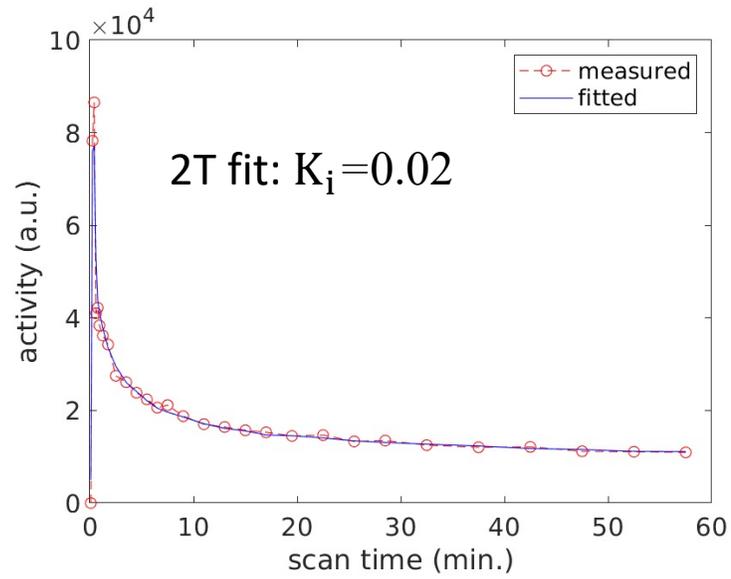
- Correction for small sample size:

$$\text{AICc} = \text{AIC} + \frac{2n(n+1)}{M-n-1}$$

Extra penalty to avoid overfitting

- AIC includes  $n$ , thus the first-order estimate of the information loss
- AICc includes  $n^2$  and is a second-order estimate
- Lower value of AIC (or AICc) indicates a better fit

# Test for Fitting a Blood TAC



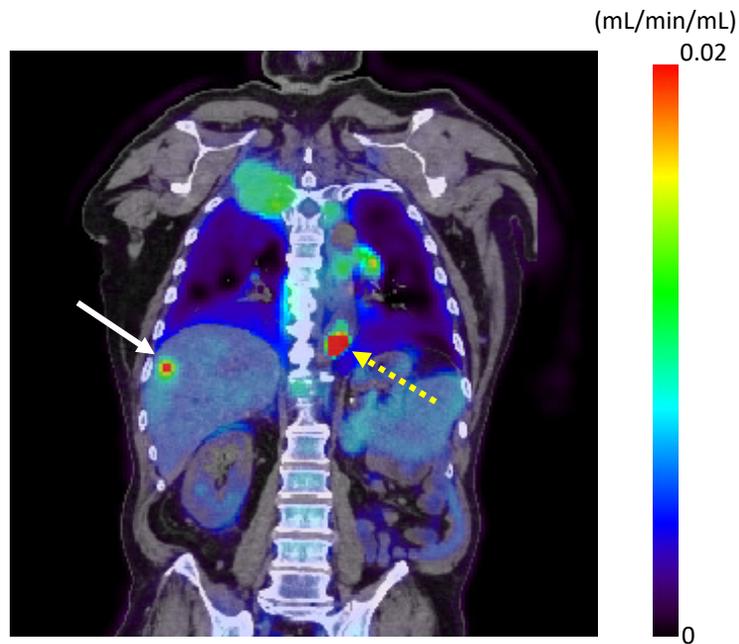
# Impact of Model Selection on $K_i$ Imaging of Lesions

Model selection map

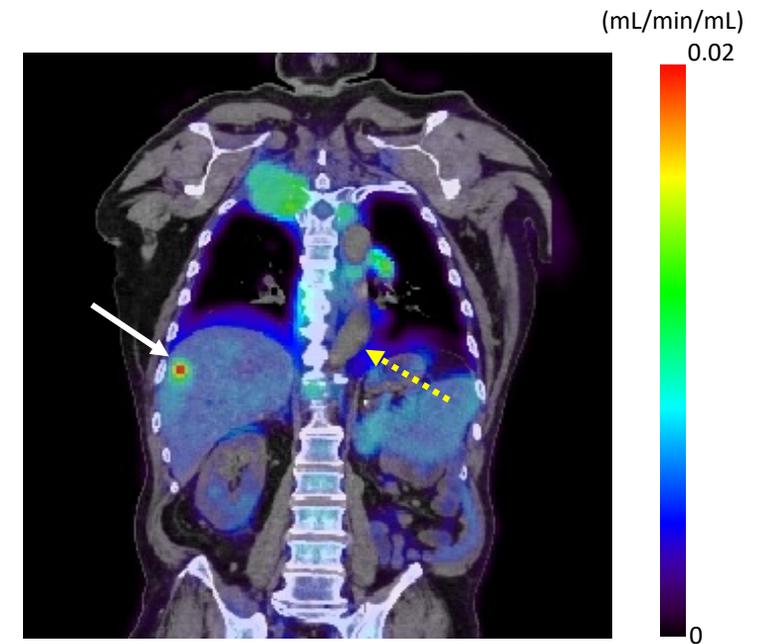


- 2Ti
- 1T
- 0T

No model selection  
(2Ti)

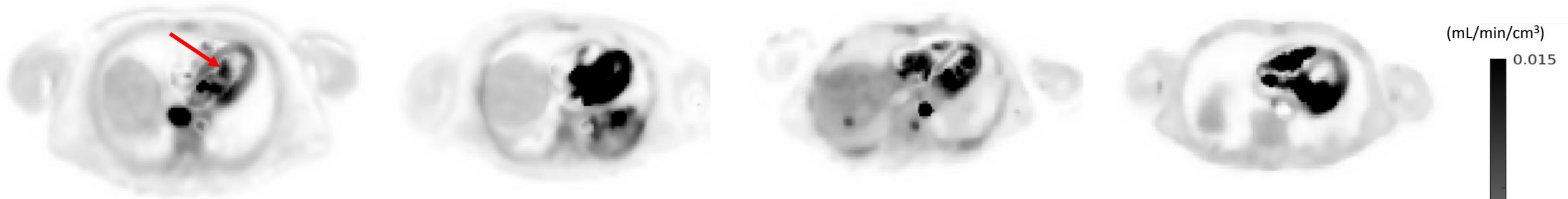


With model selection  
(0T, 1T, 2Ti)

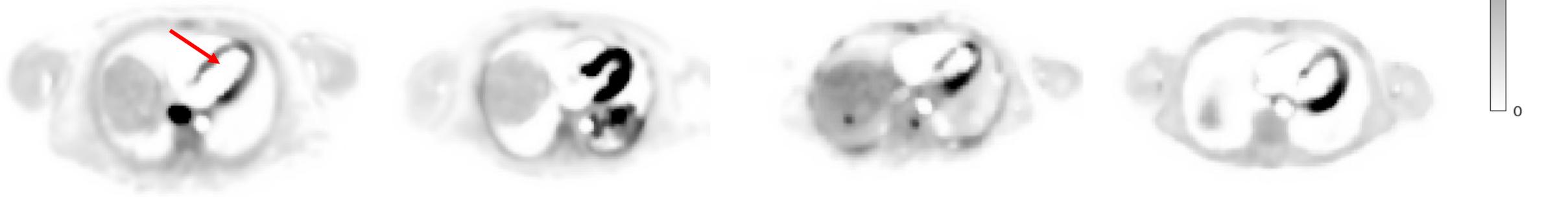


# Impact of Model Selection on Myocardial $K_i$ Imaging

No model selection

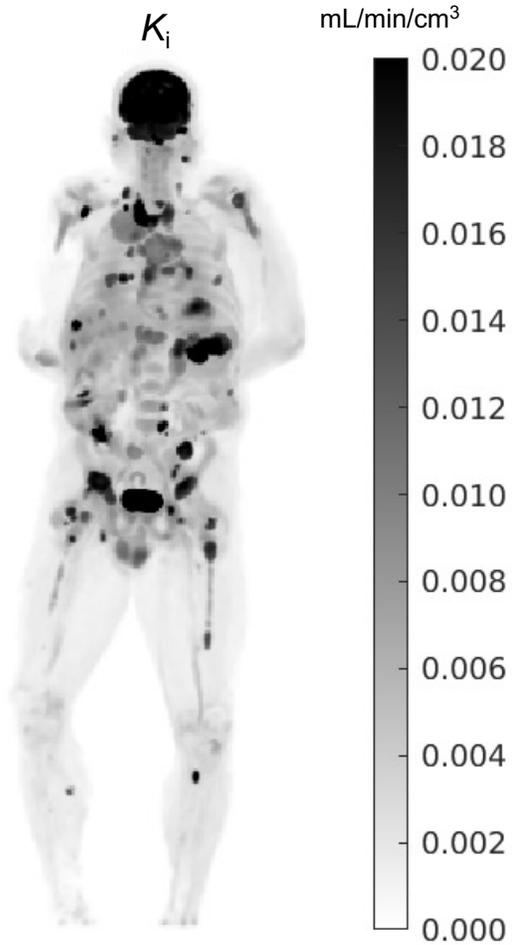


With model selection

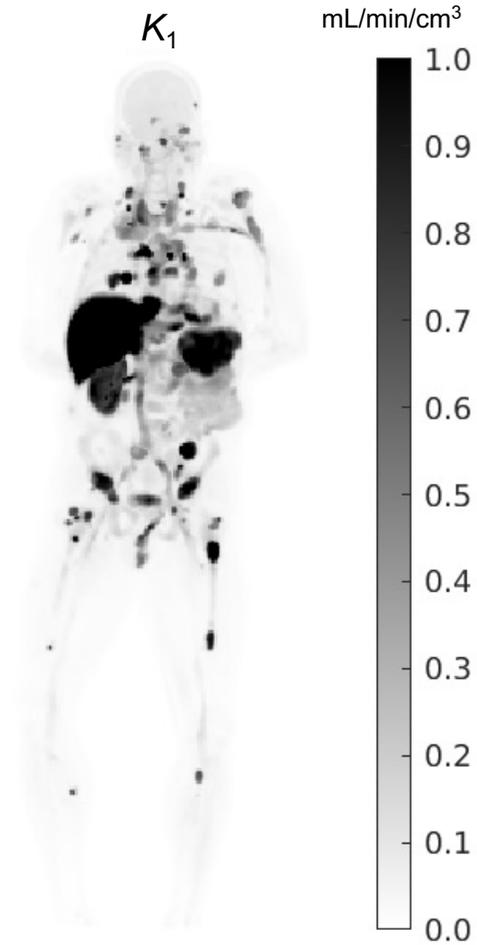


# Example of Total-Body PET Multiparametric Imaging Using Compartmental Modeling (CM)

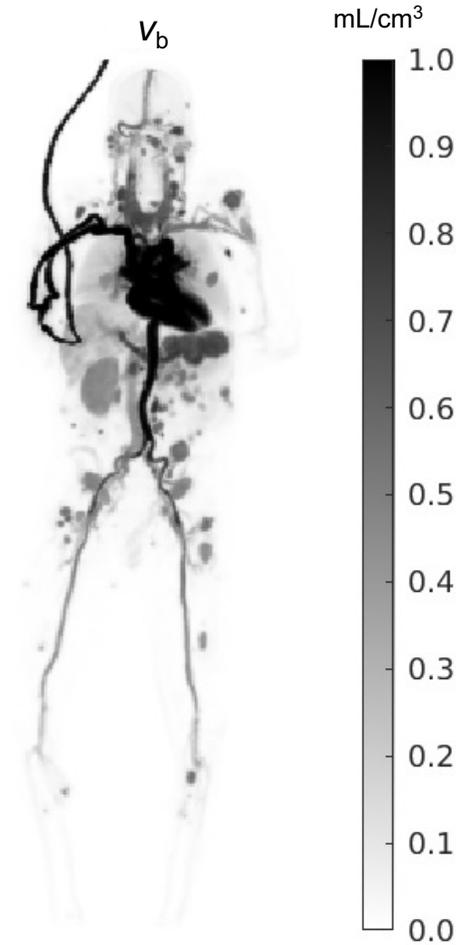
FDG net influx rate



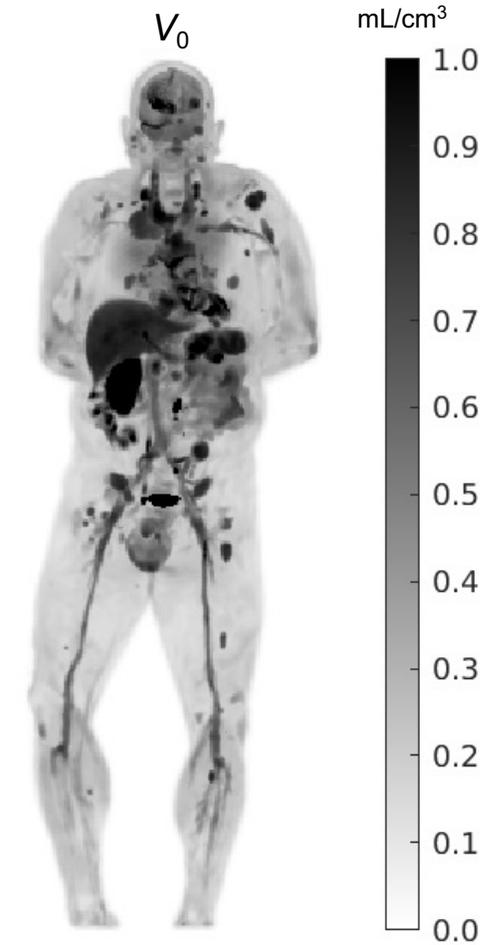
FDG delivery rate



Fractional blood volume



Volume of distribution



# Comparison of 2T CM with Patlak Plot

Irreversible 2T CM

$$C_T(t) = (1 - v_b) \text{IRF}(t; \boldsymbol{\kappa}) \otimes C_p(t) + v_b C_{wb}(t)$$

Patlak plot

$$\frac{C_T(t)}{C_p(t)} = K_i \frac{\int_0^t C_p(\tau) d\tau}{C_p(t)} + b, \quad t > t^*$$

- Pros

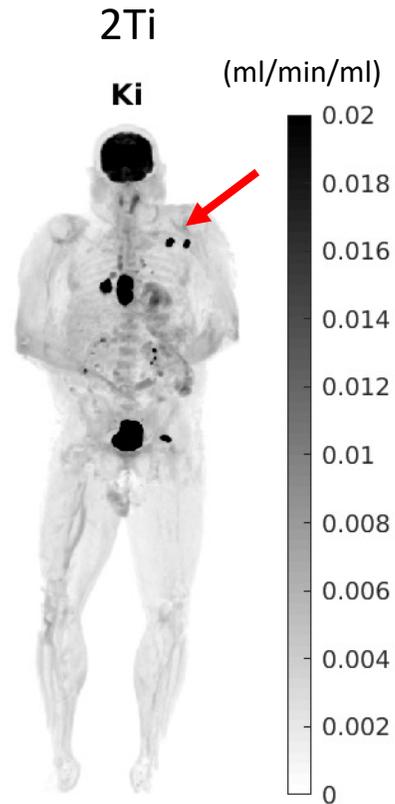
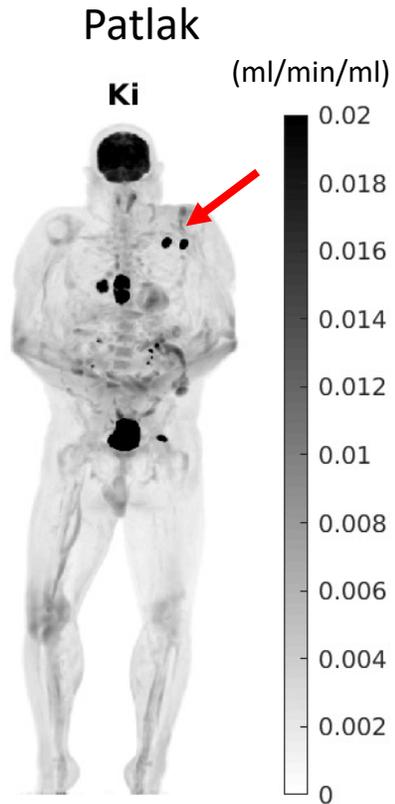
- Better modeling of the blood component ( $v_b$ )
- The Patlak slope is not exactly equal to  $K_i = \frac{K_1 k_3}{k_2 + k_3}$  of the 2T model, but  $(1 - v_b) K_i$
- Allowing parametric imaging of micro-kinetic parameters (e.g.,  $K_1$ ,  $v_b$ )

- Cons

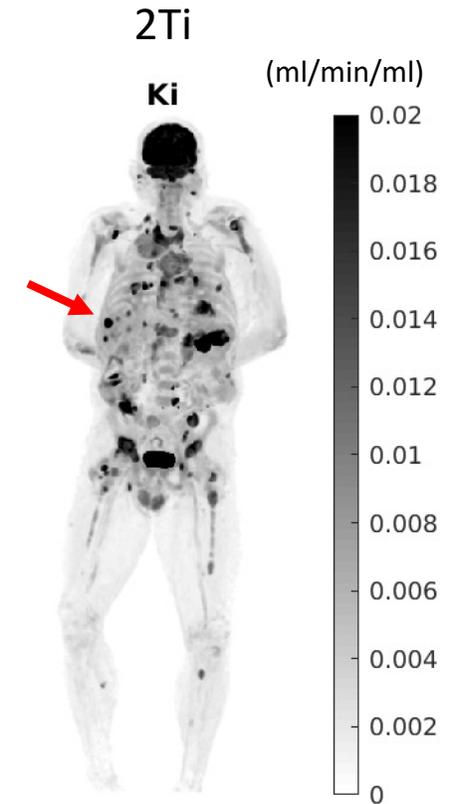
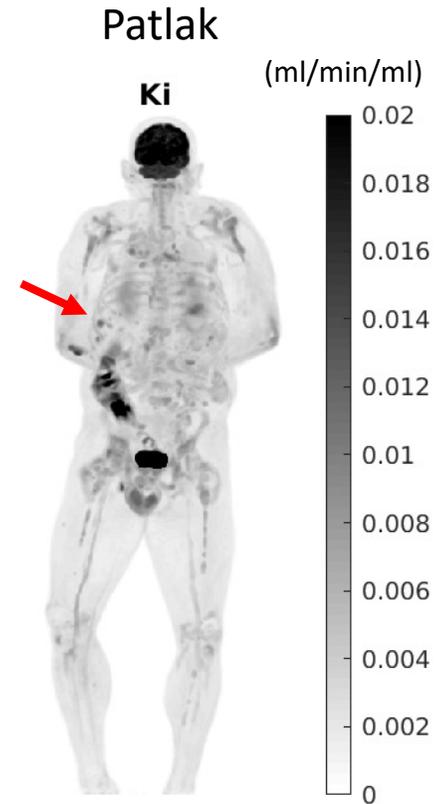
- Computationally less efficient
- Additional **corrections** are needed in order to explore the benefits

# When Similar and When Different Between Compartmental Modeling and Patlak Plot?

Similar

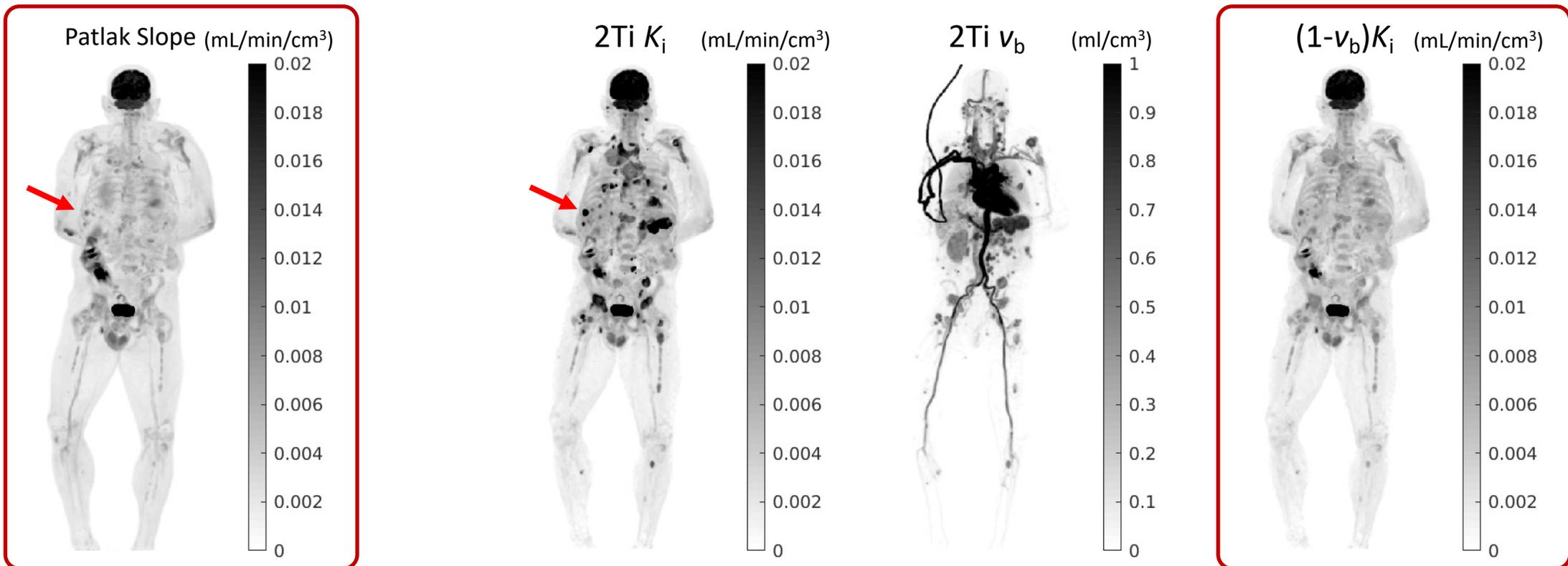


Different



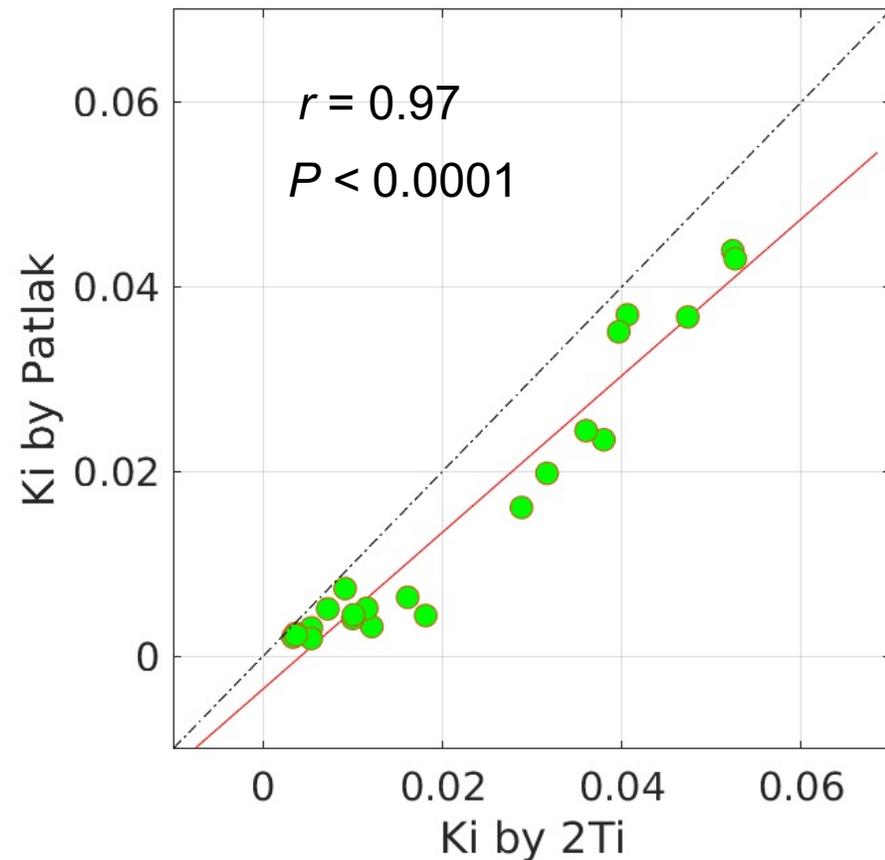
# The Relationship Depends on Vascular Fraction

- Compartment modeling allows separate estimation of  $K_i$  and  $v_b$
- Patlak slope  $\approx (1-v_b)K_i$ , which does not make the separation
- The difference becomes nonnegligible if  $v_b$  is large

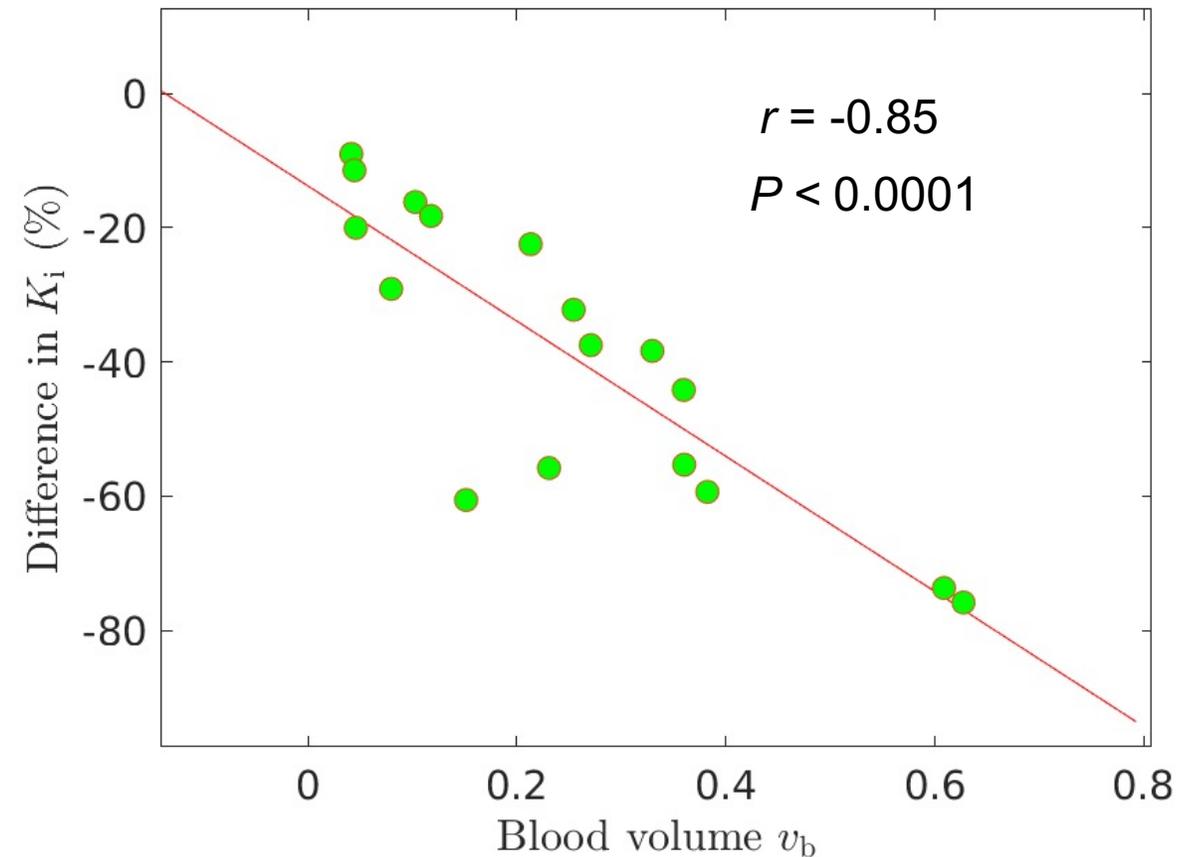


# Patlak Underestimation Correlates with Blood Volume

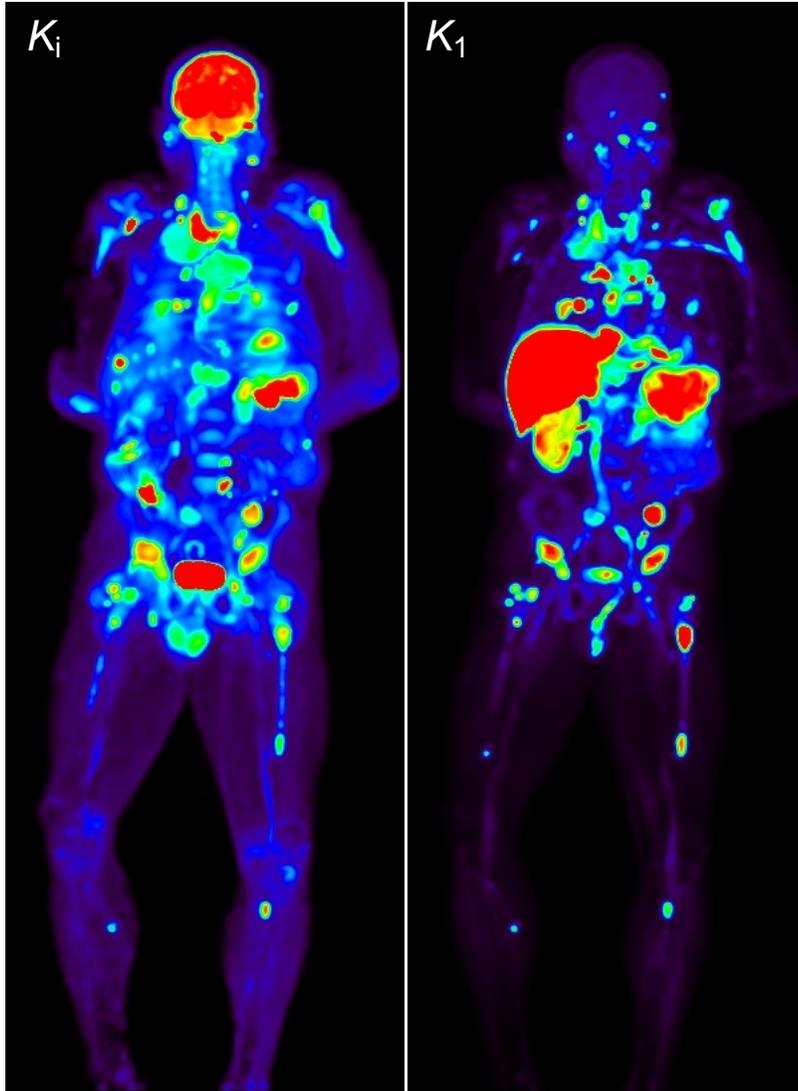
Patlak plot underestimates  $K_i$  but highly correlates with it



The underestimation is increased as blood volume increases



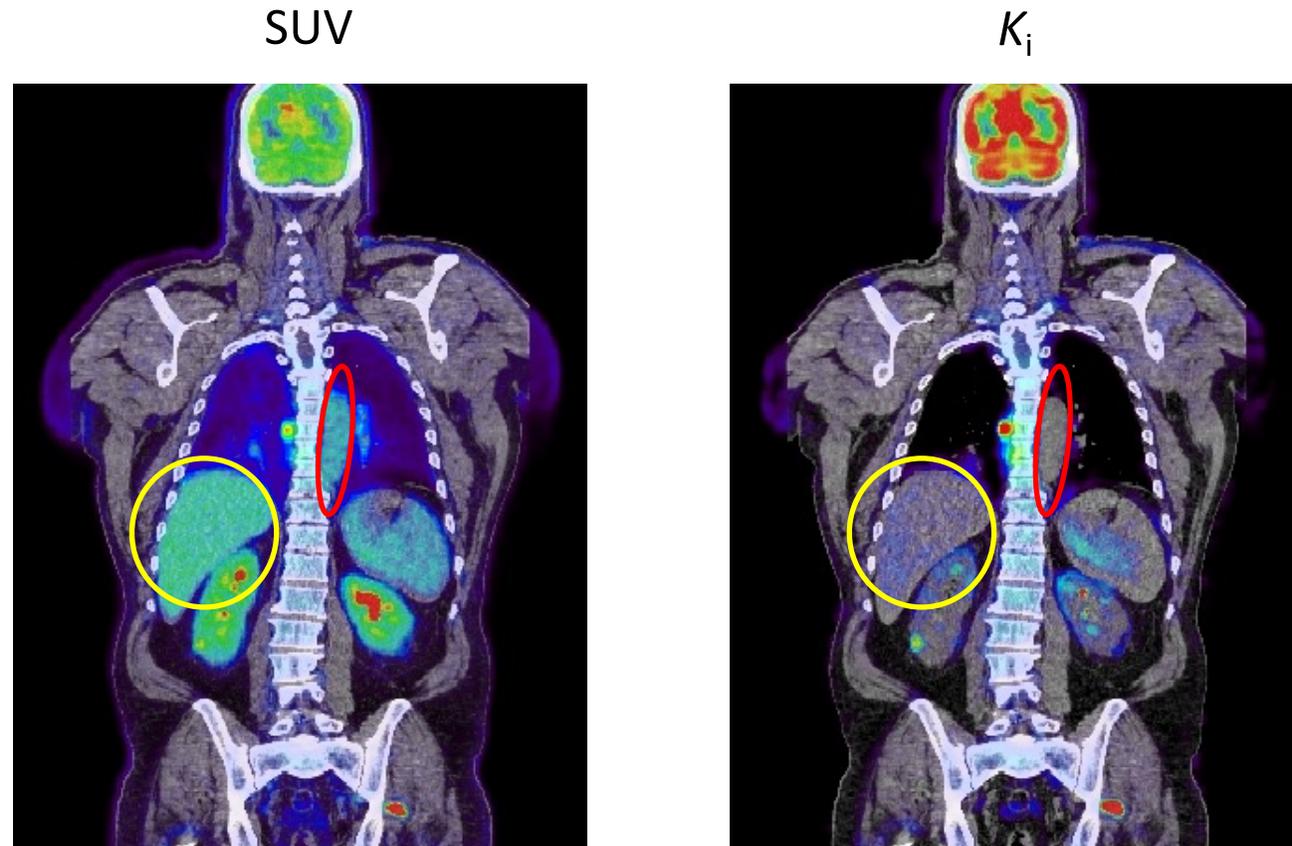
# Potential Benefits of Total-Body Multiparametric Imaging



1. Improved lesion contrast
2. Exploring micro kinetic parameters (e.g.,  $K_1$ ) for multiparametric imaging
3. Multiorgan quantification in systemic disease

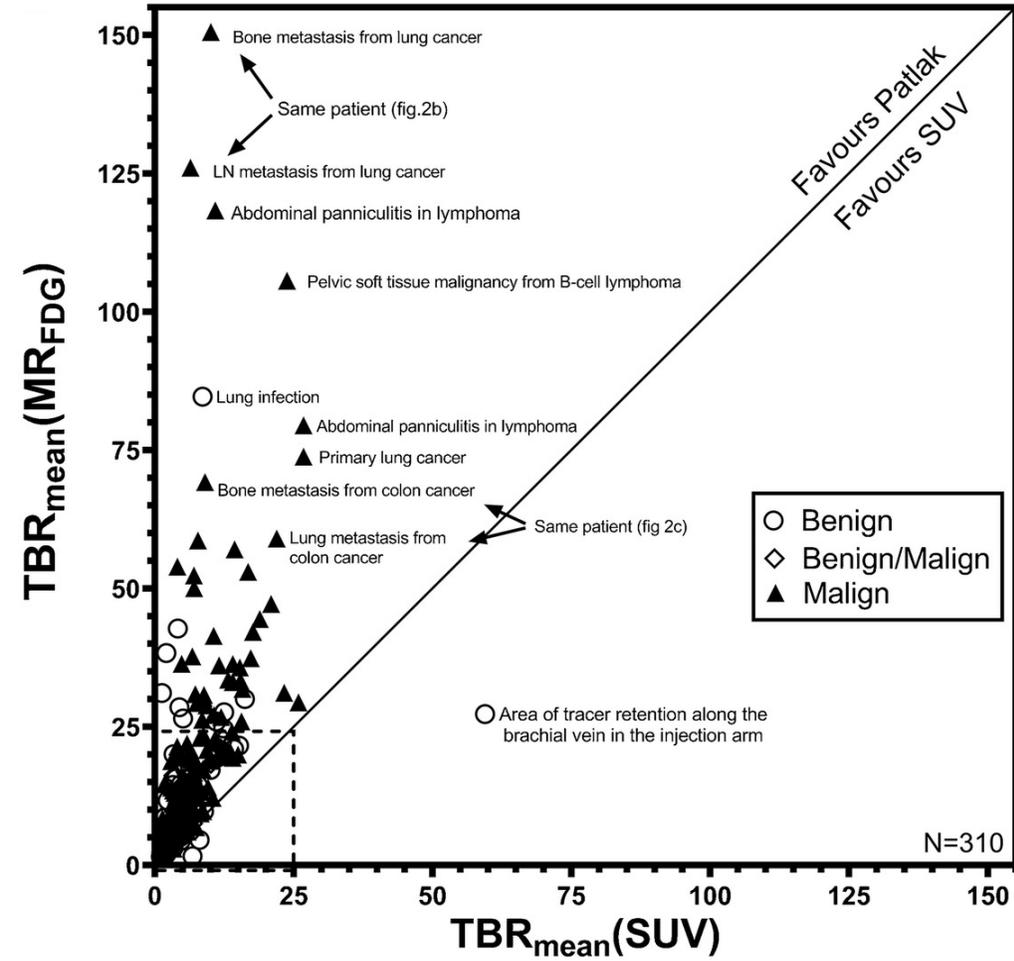
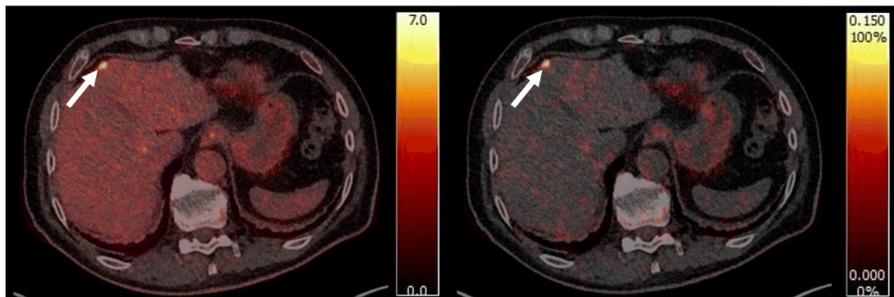
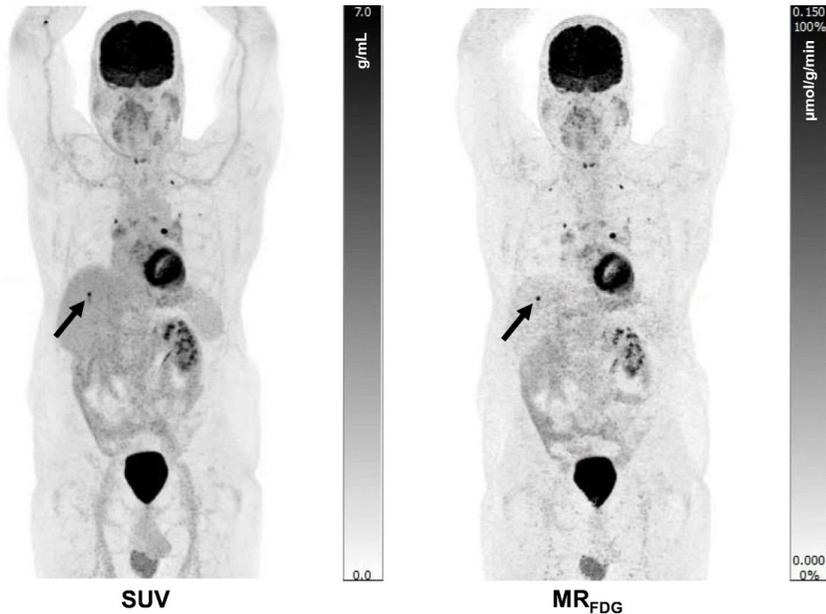
# Benefit 1: Parametric Image of $K_i$ Can Improve Lesion Contrast

- FDG  $K_i$  can clean background signal in the liver and blood pool



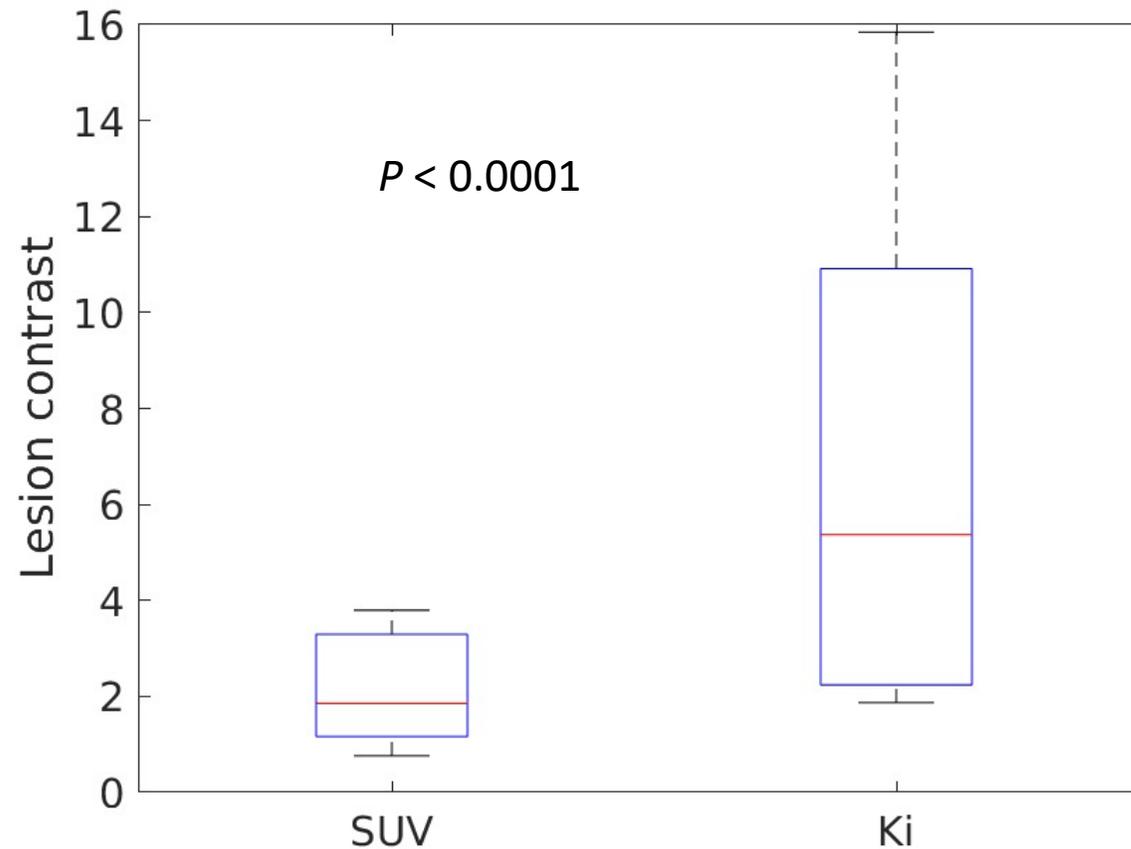
# Results from Whole-body Patlak Imaging on Conventional PET Scanners

Improved tumor-to-background ratio (TBR)



# Initial Results from Total-Body Parametric Imaging with Compartmental Modeling on EXPLORER

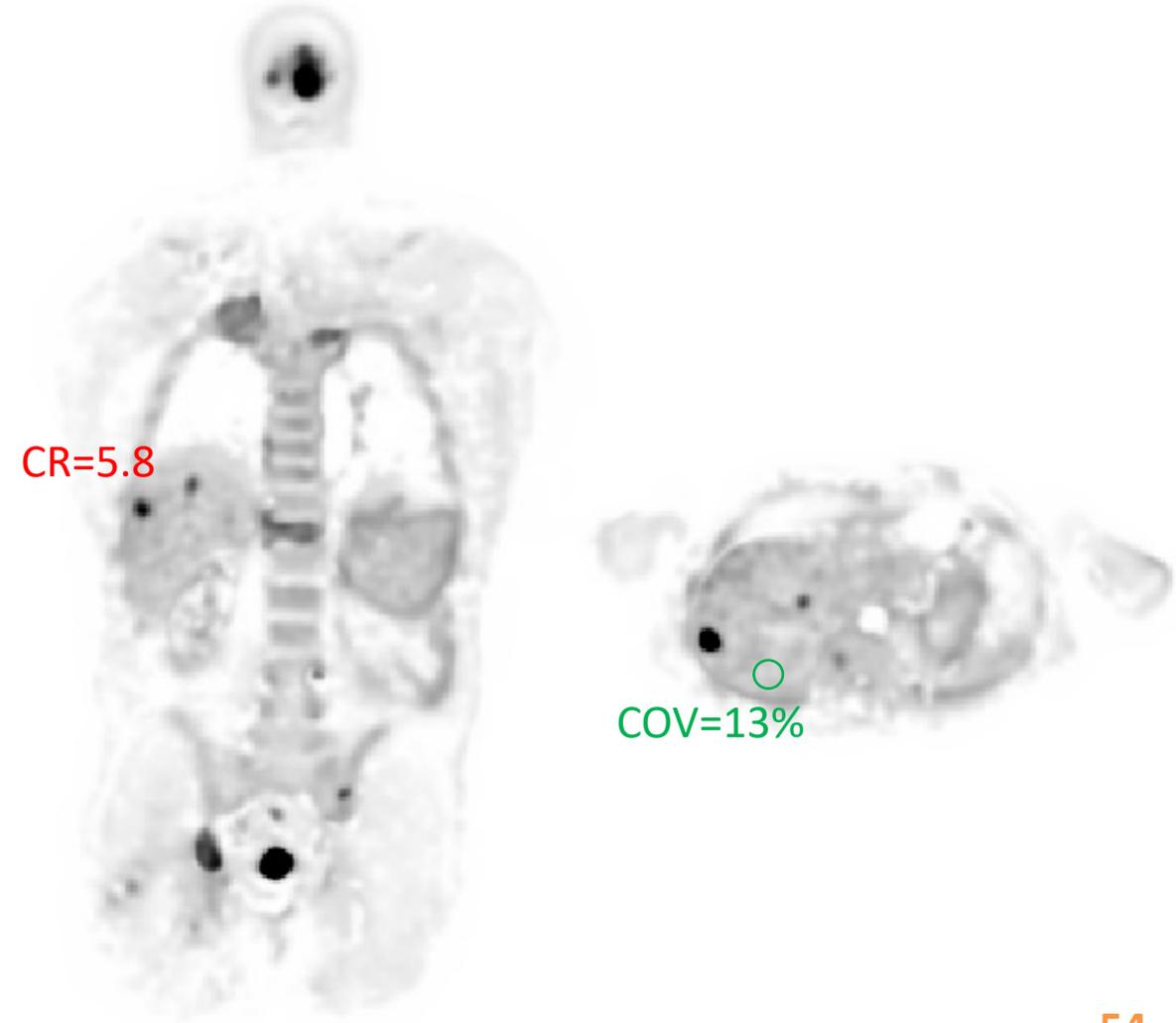
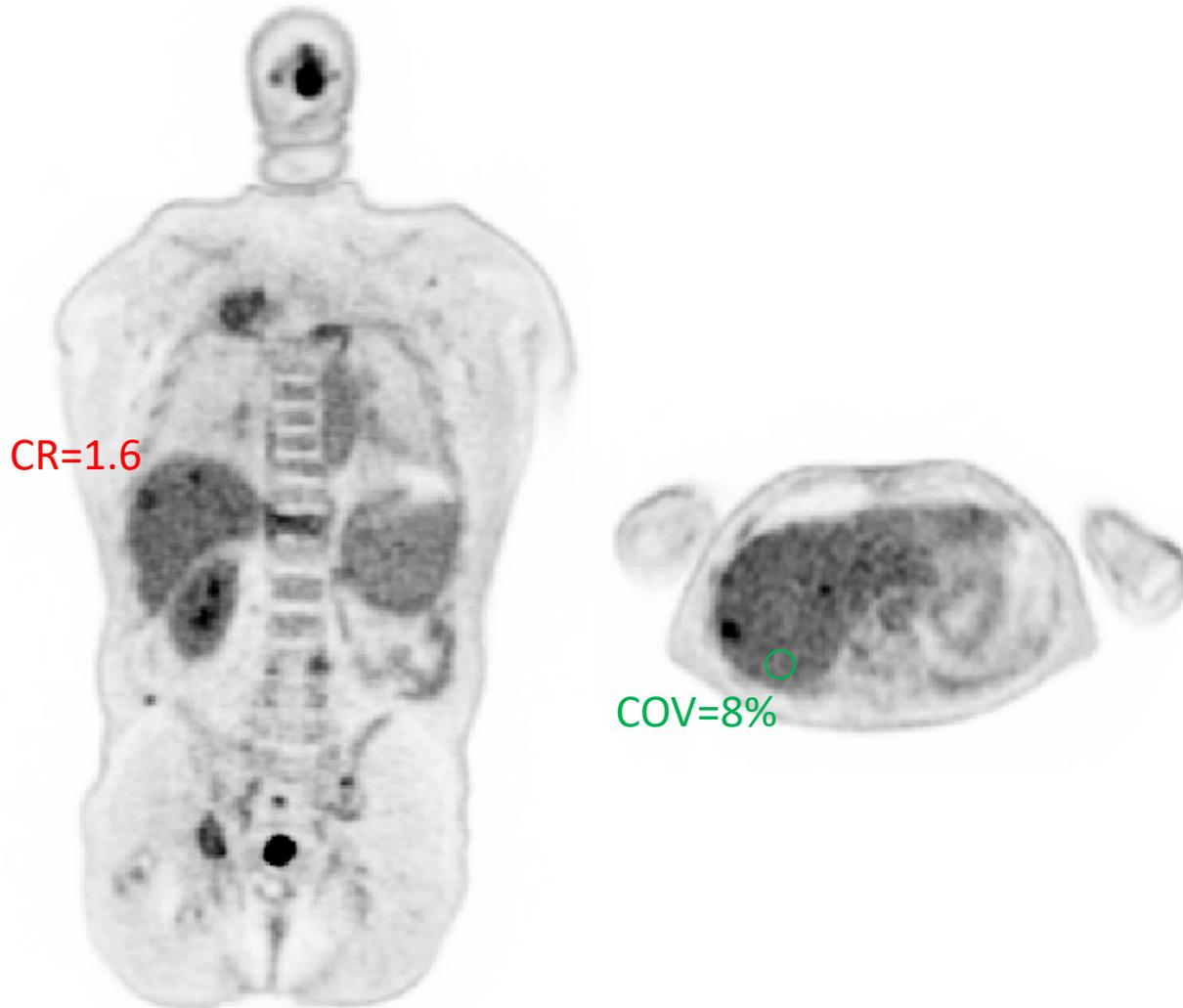
Results from 19 lesions from 5 patients with metastatic cancer



# Example of Liver Lesions

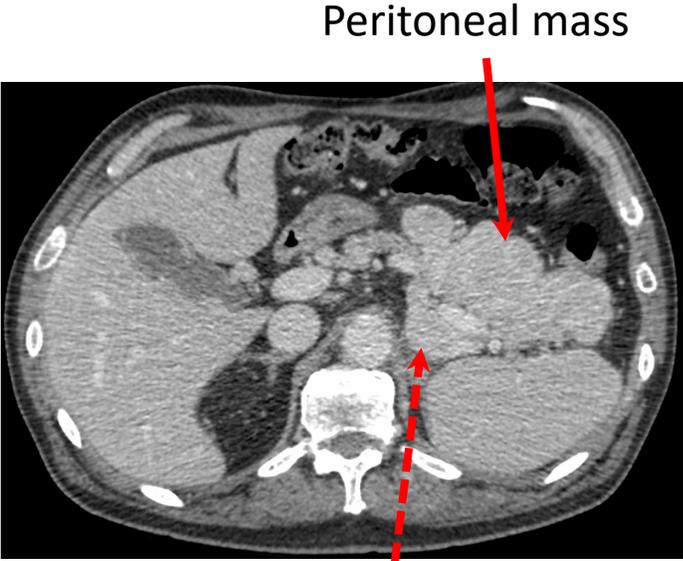
SUV

FDG influx rate  $K_i$

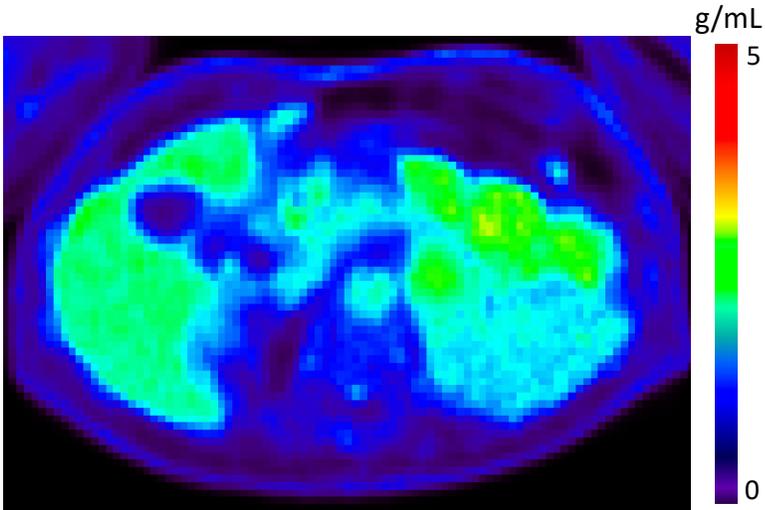


# Example of Abdominal Lesions

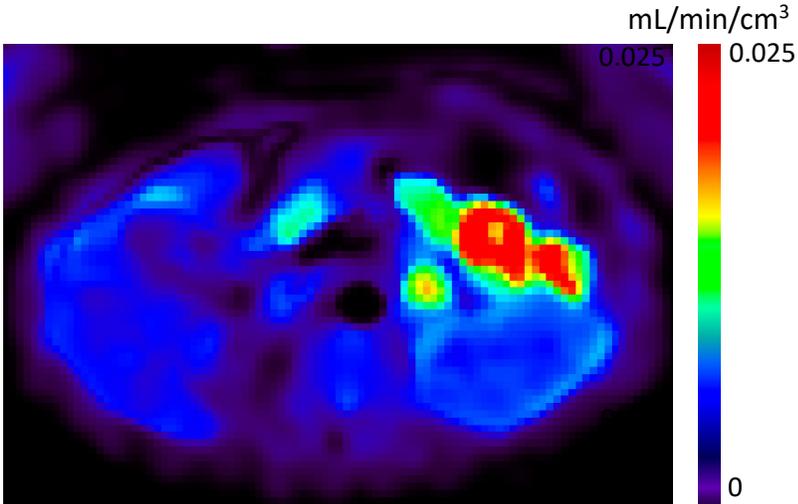
Contrast-enhanced CT



SUV

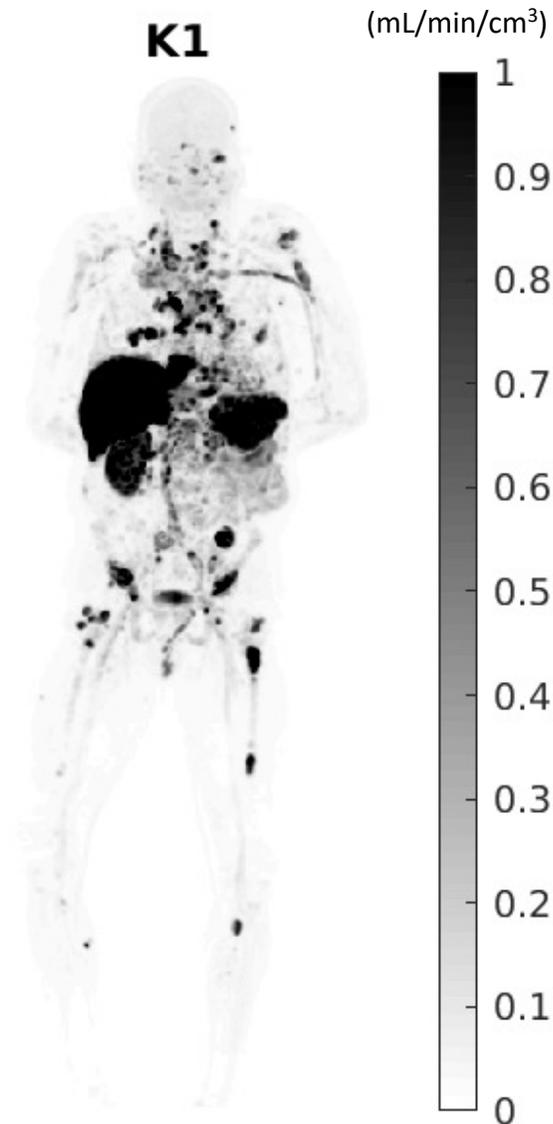


FDG  $K_i$



para-aortic lesion

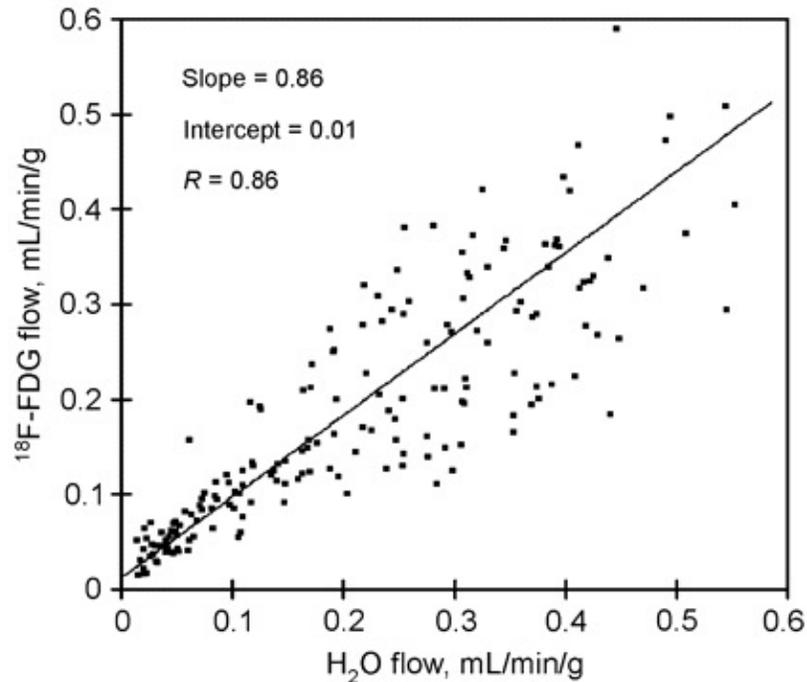
## Benefit 2: Exploring Micro-kinetic Parameters for Multiparametric Imaging



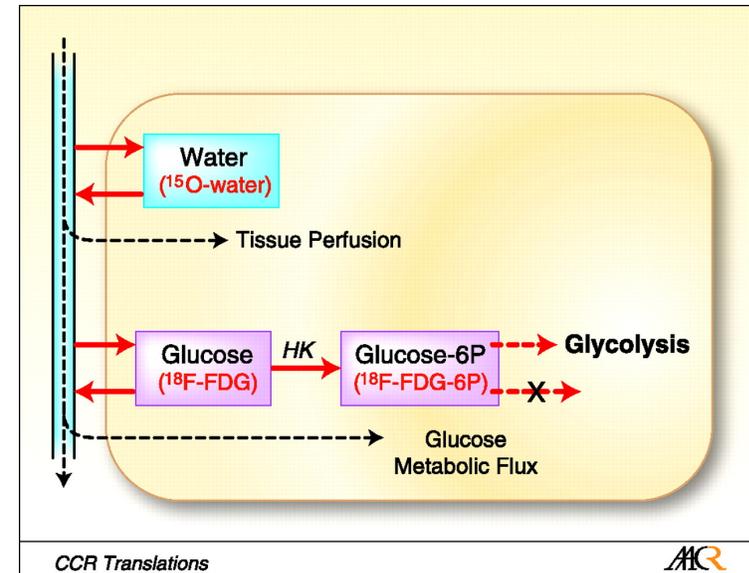
- SUV and  $K_i$  characterize glucose metabolism
- FDG delivery rate  $K_1$  generally reflects a mix of blood flow and glucose transport
- Many potential applications of FDG  $K_1$ :
  - Serve as a surrogate of blood flow
  - Independent imaging biomarker
  - Create lesion contrast

# Cancer: FDG $K_1$ May Highly Correlate with Tumor Blood Flow

- Due to generally high extraction fraction of  $^{18}\text{F}$ -FDG in tumors



- Enabling single-tracer imaging of **tumor flow-metabolism mismatch**



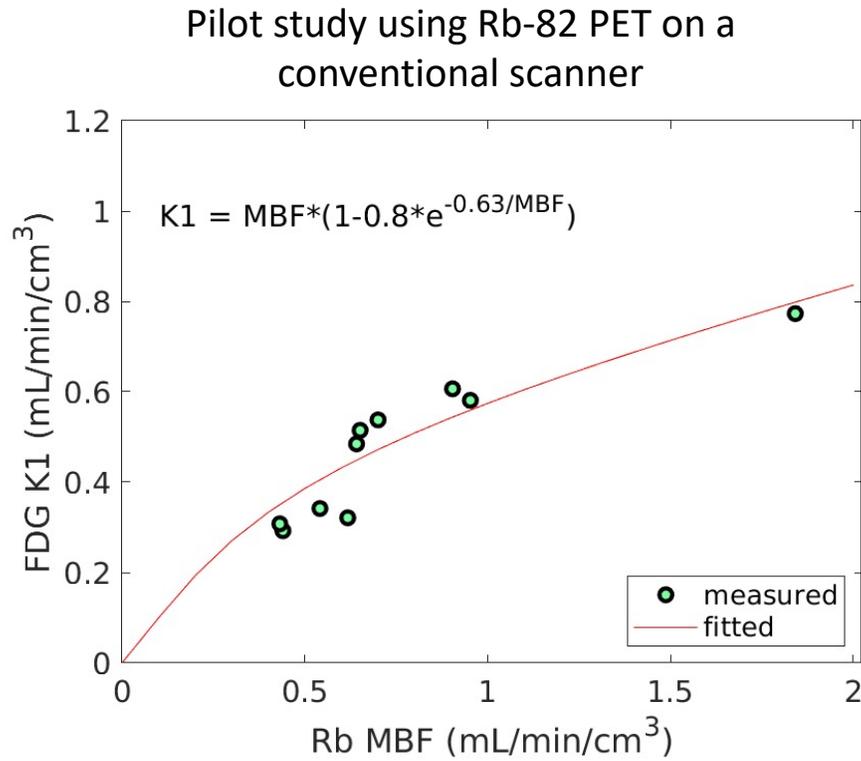
Mankoff *et al* CCR 2009

FDG flow: Mullani *et al*, JNM 2008; Tseng *et al* JNM 2004;

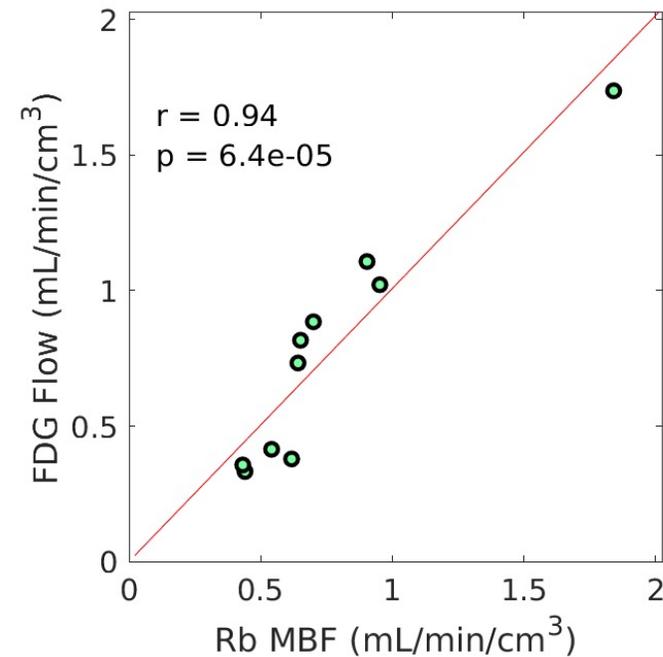
Flow-metabolism mismatch: Komar *et al* CCR 2009; Mankoff *et al* CCR 2009

# Heart: Measuring Myocardial Blood Flow (MBF) Using FDG $K_1$

- FDG  $K_1$  is closely associated with blood flow in the myocardium

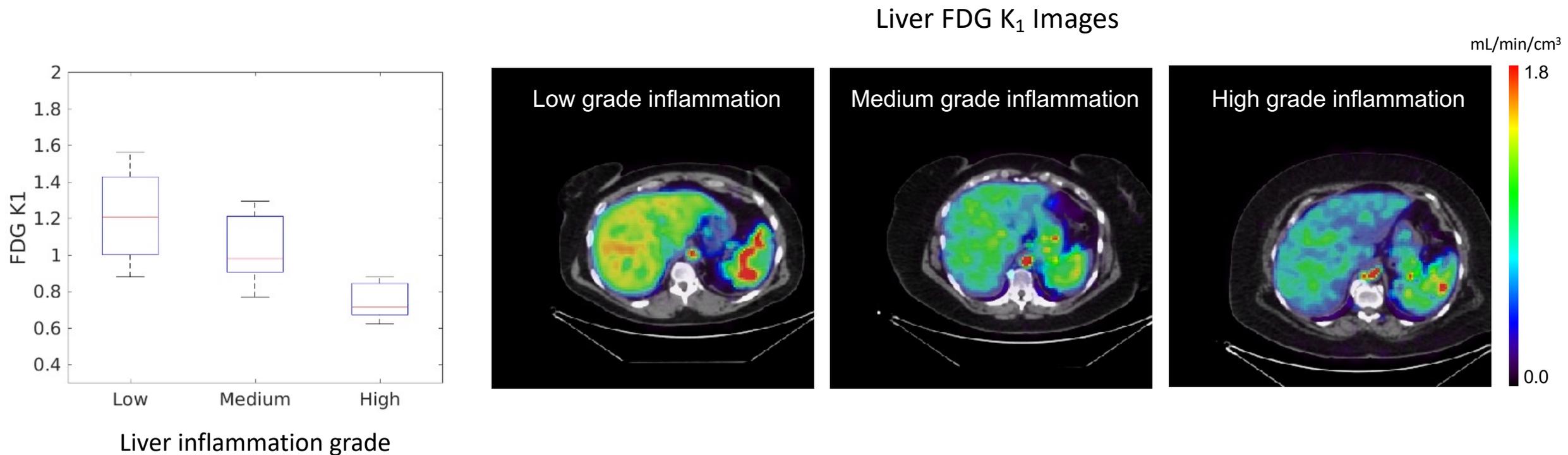


- Correlation of FDG-derived MBF with Rb MBF after the nonlinearity correction

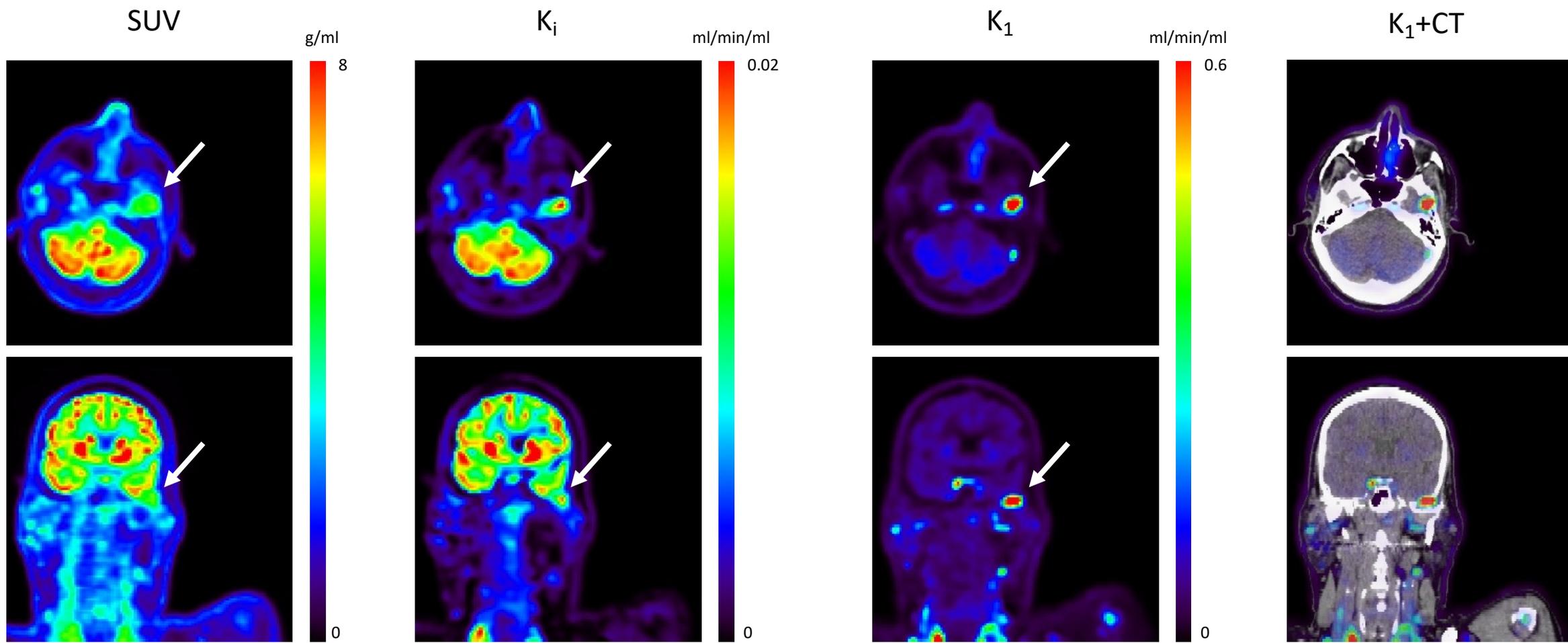


# Liver: FDG $K_1$ May Be a Potential Biomarker of Liver Inflammation

- Decreased liver FDG  $K_1$  is associated with increased liver inflammation



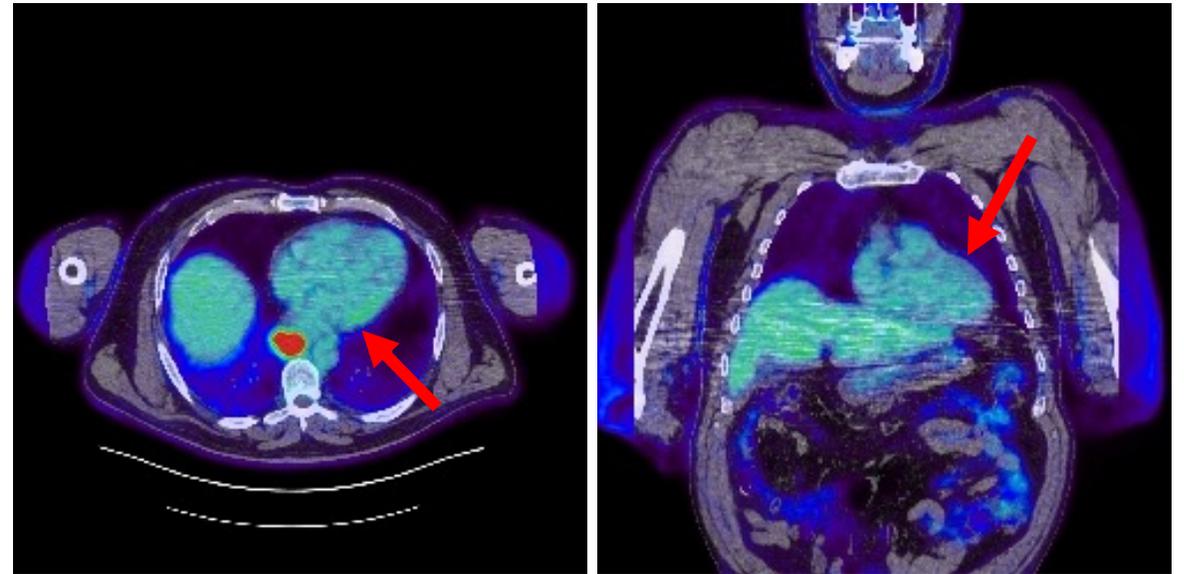
# Brain/Skull: FDG $K_1$ Has Potential to Better Detect Tumors



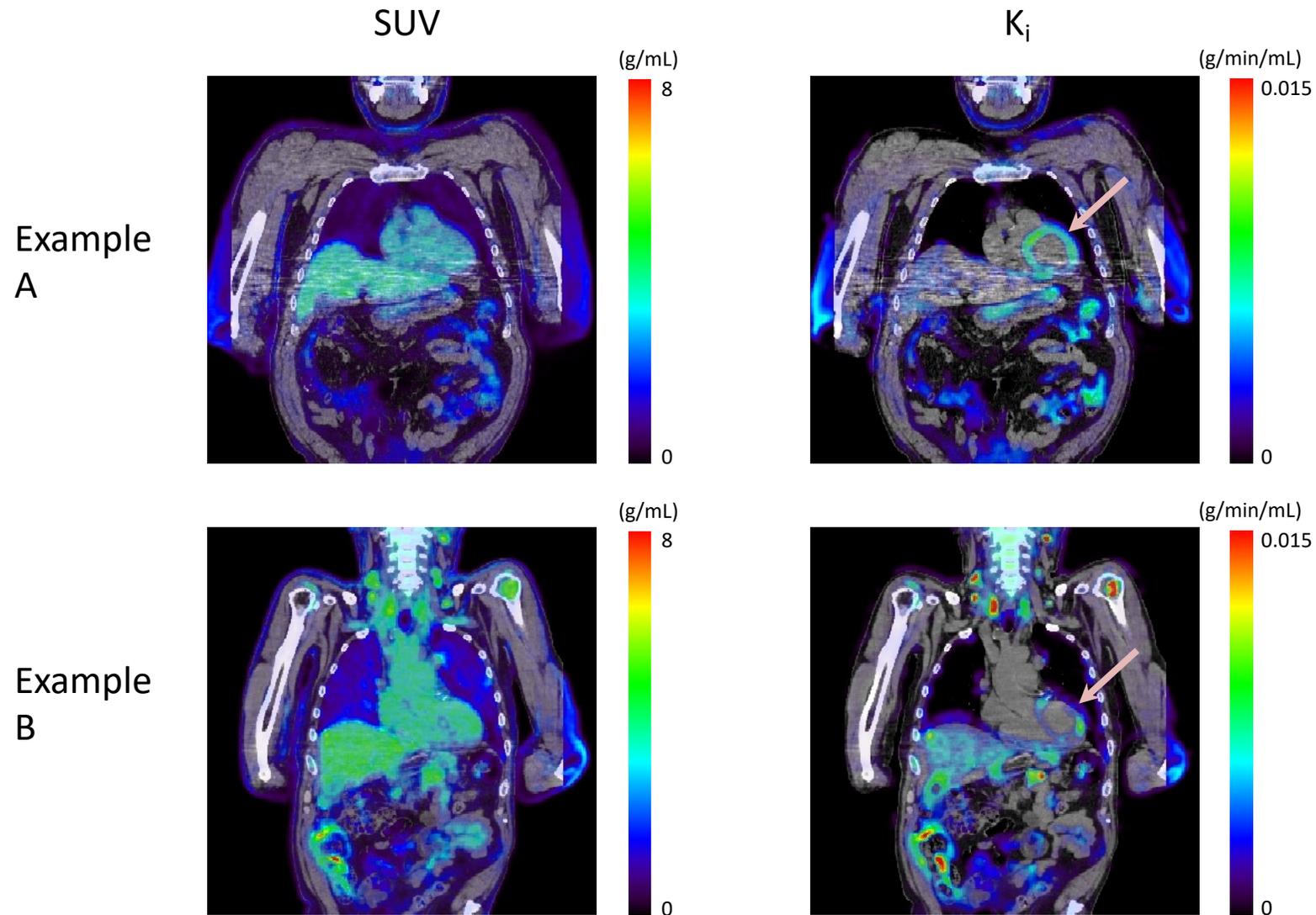
# Benefit 3: Enabling Multi-Organ Evaluation in Systemic Disease

- Simultaneous evaluation of myocardium in cancer patients?
- **Problem:** 30-40% of standard oncological FDG-PET scans do not show visible myocardium
- Parametric imaging can help

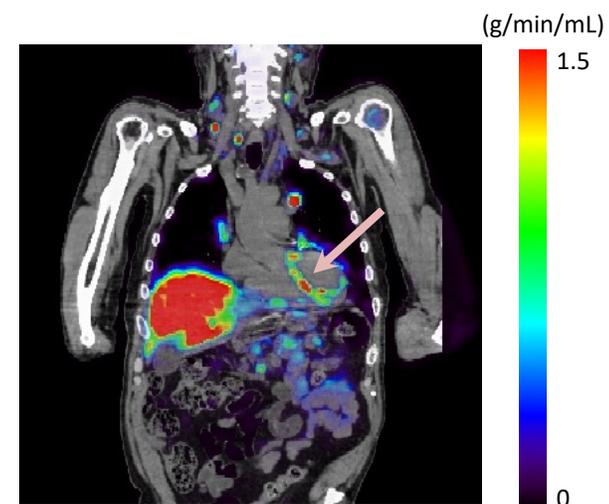
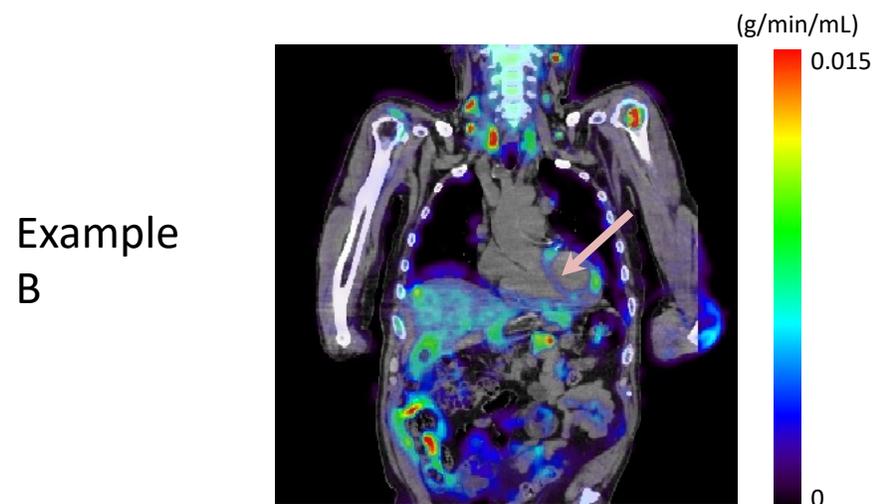
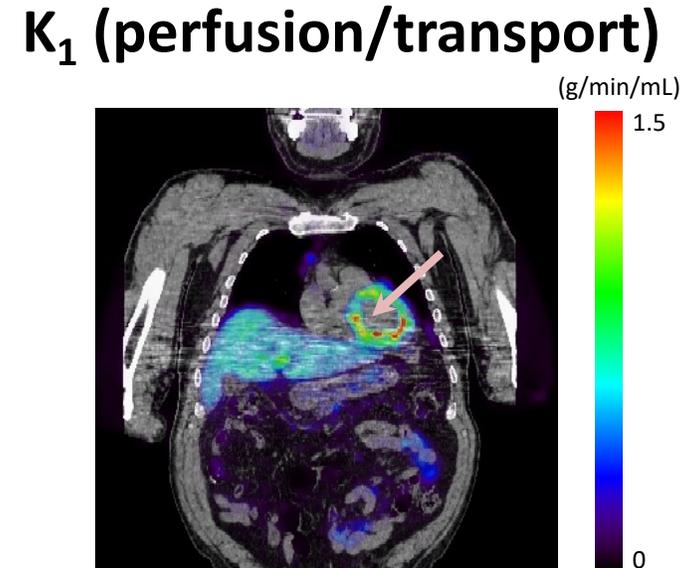
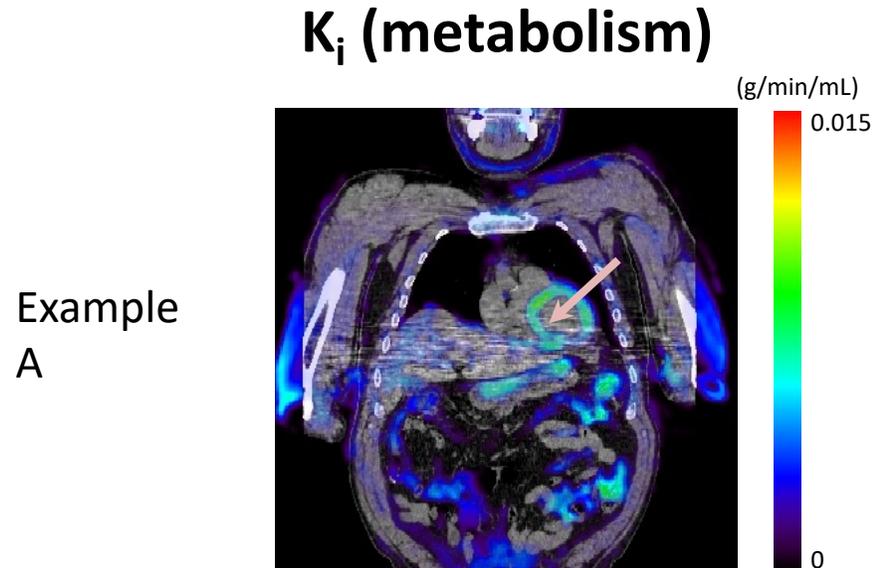
SUV (60 min. p.i.)



# Simultaneous Visualization of Myocardium by Parametric Imaging

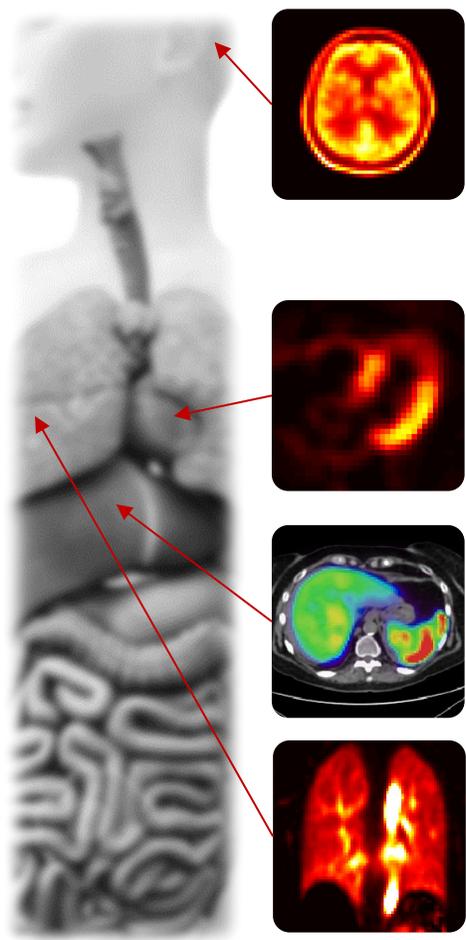


# Allowing Evaluation of Perfusion-Metabolism Coupling/Mismatch



# Putting All Puzzles Together

## Single-tracer ( $^{18}\text{F}$ -FDG) Multiorgan Multiparametric Evaluation by EXPLORER



### Multi Organs

- Myocardium
- Liver
- Lung
- Brain
- Bone marrow
- Spleen
- Kidney ...

### Multiparametric Imaging

- Glucose metabolism
- Glucose transport / perfusion
- and potentially more

# Advanced Topics in Total-Body Modeling and Analysis

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- Metabolite correction using total-body compartmental modeling
- Motion correction for total-body parametric imaging
- High-temporal resolution (e.g., 1s/frame) kinetic modeling
- 4D parametric imaging with cardiac/respiratory modulation
- Total-body dual-tracer and multi-tracer dynamic imaging
- Total-body organ network analysis and connectomes
- and many more ...

Thank you for your attention!

Questions?

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